TASI/PiTP/ISS Lectures On Moduli and Microphysics

Eva Silverstein*

Abstract

I review basic forces on moduli that lead to their stabilization, for example in the supercritical and KKLT models of de Sitter space in string theory, as well as an $AdS_4 \times S^3 \times S^3$ model I include which is not published elsewhere. These forces come from the classical dilaton tadpole in generic dimensionality, internal curvature, fluxes, and branes and orientifolds as well as non-perturbative effects. The resulting (A)dS solutions of string theory make detailed predictions for microphysical entropy, whose leading behavior we exhibit on the Coulomb branch of the system. Finally, I briefly review recent developments concerning the role of velocity-dependent effects in the dynamics of moduli. These lecture notes are based on material presented at various stages in the 1999 TASI, 2002 PiTP, 2003 TASI, and 2003 ISS schools.

1. Introduction and Motivation

The large scale dynamics of the universe (including the question of whether the universe is large at all in a given model) is determined to a significant extent by the cosmological term in the effective action. In a theory such as string theory with scalar fields, this term is in general a nontrivial function of the scalar field VEVs, which in turn determine

^{*} SLAC and Department of Physics, Stanford University, Stanford, CA 94309

the coupling constants appearing in low energy particle physics in each vacuum. Acceleration of the universe is obtained if the scalar fields roll slowly enough that their kinetic energy is dominated by their potential energy.¹ This situation can arise if the moduli are stabilized or metastabilized, if the potential is very flat, or if significant interactions slow down the scalar motion.

The observed geometry of the universe suggests two phases of accelerated expansion—one in the past (inflation) and one beginning to dominate now. Observations also strongly bound time evolution of fundamental constants, and extra scalar gravitational-strength forces. It is therefore important to determine the contributions to the cosmological term and understand how the scalar fields become stabilized. It has recently become clear that other effects dependent on the scalar field velocities can play a large role in their dynamics, and it is important to incorporate these kinetic effects as well. In this set of notes, I will review some of the recent progress concerning the stabilization of moduli and the resulting physics of dark energy and inflation. While there has been much progress, there are also larger open problems—both conceptual and technical—making this a valuable subject to get into at this stage.

Although the cosmological term is dominant at long distances, it is sensitive to microphysics in various ways. Firstly, the quantum corrections to the cosmological term are UV sensitive, coming at the scale of SUSY breaking (which may be anywhere from the TeV scale up to the string or Planck scale). Secondly, the forces available to fix the moduli depend on the possible ingredients in the theory; for example string theory in a given background determines the spectrum of low energy fields and in principle determines the zoo of branes and other defects which are consistent physical objects within the theory. Finally, as in black hole physics, there is some evidence that solutions with positive cosmological constant have an associated horizon entropy and temperature.² If it is accounted for by microphysical degrees of freedom, this may provide a dual description of the dark energy, or some aspects of it, in terms of the degrees of freedom of string theory.

For all these reasons, it is important to get a handle on moduli stabilization and microphysics. In what follows, I will overview some basic aspects of this subject. I will

which is not precisely the same condition as the "slow roll conditions".

² Here we will find metastable solutions with positive cosmological constant, so these thermodynamic parameters are at best approximate; however one finds that equilibrium can be attained in a much shorter time than the decay time out of the metastable vacuum.

not reproduce all of the calculations I covered in the lectures, leaving out some of the ones readily available in existing papers but including here a set of simple but important computations required for getting started in this area. I will otherwise try to provide an overview of the works I covered in the lectures, emphasizing some points that are especially important and sometimes confusing to those entering this area of research.³

2. Basic Contributions

In this section we will catalogue a number of contributions to the moduli potential. In a generic situation, these contributions will all be involved (plus others not covered here, depending on the circumstances). As we will see, there are more than enough contributions to provide balancing forces on all the moduli, and we expect the moduli to be fixed in many cases, leading to dS or AdS solutions.

Before delving into the detailed contributions, let us start by noting some important generalities concerning moduli stabilization, including the rescaling to Einstein frame and the behavior of the moduli potential near large radius and weak coupling limits. Then we will list a bunch of important contributions to the 4d potential energy, and note how they scale with moduli. We will discuss the issue of tachyons, and briefly introduce the method of fixing moduli by orbifolding. In §3, we will put various subsets of these ingredients together to provide compensating forces on the moduli.

2.1. General Considerations

One basic but important aspect to keep track of is the "frame". It is often most convenient to rescale the metric so that the Einstein term $\int \sqrt{g} \mathcal{R}$ in the action has no moduli dependence in its coefficient. This is not what arises immediately from dimensional reduction and perturbative string calculations. For example, the worldsheet path integral leads to tree level amplitudes in closed string theory, such as those determining the Einstein-Hilbert term in the Lagrangian, which arise at order $1/g_s^2$ in terms of the string coupling g_s (i.e. coming with a power of $e^{-2\Phi}$ where Φ is the dilaton). In the presence of moduli dependence in the Einstein term—of the general form $\int f(\phi_I)\mathcal{R}^{(s)}$ —the problem of

³ It is also practically impossible to include all the important references here, but I hope to have included a representative sample of the recent (as well as some older) efforts in this direction. Earlier TASI lecture notes on moduli and cosmology, such as [1] are also available.

solving the equations of motion for the scalars ϕ_I has an extra tadpole from the spacetime curvature.

Instead, as we will derive presently, we can remove this dependence by working with a rescaled metric to obtain the canonical Einstein term $\int \sqrt{g_E} \mathcal{R}_E$ where the subscript E refers to the Einstein frame. Then the scalar field equation will be simply $\partial_{\mu}(\sqrt{g_E}g_E^{\mu\nu}\partial_{\nu}\phi^I) = -\partial_I \mathcal{V}_E(\phi) = 0$ where \mathcal{V}_E is the Einstein frame potential energy.

Start in the D-dimensional string frame, for some D > 4 which we plan to compactify down to four dimensions (or more generally down to some other dimension d in toy models). The action in string frame is

$$S = \int d^D x \sqrt{g_s^{(10)}} \frac{e^{-2\Phi}}{l_s^8} \mathcal{R}_s + \dots$$
 (2.1)

where l_s is the string length, i.e. the square root of the inverse string tension. Reducing this to four dimensions, on a D-4 dimensional space X of volume $l_s^{D-4}V_X$, we obtain

$$S = \int d^4x \sqrt{g_s^{(4)}} \frac{e^{-2\Phi} V_X}{l_s^2} \mathcal{R}_s + \dots$$
 (2.2)

Now let us write $e^{\Phi} = g_s e^{\tilde{\Phi}}$ and $V_X = V_{X0} \tilde{V}_X$, with g_s, V_{X0} constant and with the four dimensional Planck length defined by

$$l_4^2 = l_s^2 \frac{g_s^2}{V_{\chi_0}^2} \tag{2.3}$$

This leaves $\tilde{\Phi}$ and \tilde{V}_X as fluctuating scalars in four dimensions, the dependence on which we wish to remove from the Einstein term. We can do this by rescaling the four dimensional metric via

$$g_{\mu\nu,s}^{(4)} \equiv \frac{e^{2\tilde{\phi}}}{\tilde{V}_X} g_{\mu\nu,E}^{(4)} \tag{2.4}$$

which defines the Einstein frame metric $g^{(4)}_{\mu\nu,E}$. With this rescaling, our action has become

$$S = \int d^4x \sqrt{g_E^{(4)}} \frac{1}{l_4^2} \mathcal{R}_E \tag{2.5}$$

with the dimensionful coupling $l_4^2 = G_N$ appearing as it should but with all scalar field dependence removed. This rescaling similarly removes the $e^{-2\Phi}$ dependence in front of the Φ kinetic term, which leaves us with an exponential potential in terms of the canonically normalized field, as we will see next.

As I alluded to above, this rescaling affects also the form of the potential energy, in an important way. Namely the string-frame action dimensionally reduced to four dimensions also contains potential energy terms, which will be one of our main concerns in these notes. If we write the potential energy term in the action as

$$\int d^4x \sqrt{g_s^{(4)}} \frac{1}{l_s^4} \mathcal{V}_s^{(4)} \tag{2.6}$$

(i.e. defining $\mathcal{V}_s^{(4)}$ to be the string frame potential energy in string units), it becomes in terms of the Einstein frame metric

$$\int d^4x \sqrt{g_E^{(4)}} \frac{1}{l_4^4} \frac{e^{4\Phi}}{V_X^2} \mathcal{V}_s^{(4)} \tag{2.7}$$

Here we used the rescaling (2.4) in the \sqrt{g} factor in (2.6), and also wrote the expression in terms of the 4d Planck length l_4 rather than the string length l_s .

So finally we can identify the four dimensional Einstein frame cosmological term to be

$$\Lambda_E^{(4)} = \frac{1}{l_4^2} \frac{e^{4\Phi}}{V_X^2} \mathcal{V}_s^{(4)} \tag{2.8}$$

Similar comments would apply to any situation with a function f of moduli multiplying the curvature; one can transform to Einstein frame via the relations (2.4)(2.8) with the replacement of $V_X/e^{2\Phi}$ by f.

The resulting volume and coupling dependence in the potential in Einstein frame leads to an important feature of the physics: all sources of energy coming from local physics on the compact space scale to zero as the coupling approaches zero and/or the volume approaches infinity (as discussed in more detail in e.g. [2][3]). Even if there is an energy density filling the full D-dimensional spacetime, the two powers of V_X arising in the denominator from the conversion to Einstein frame beat the power of V_X from integrating the D-dimensional energy density, producing a contribution that approaches zero as $V_X \to \infty$.

As a result, in order to stabilize the moduli expanding about a controlled weakly coupled and/or large radius solution, one requires both negative and positive sources of potential energy, with sufficiently large coefficients in front of the subleading terms in the expansion to produce a balance of forces within the weakly coupled regime.

In addition to these runaway moduli, there are in general also periodic moduli, coming from integrated p-1-form potentials. Although they cannot run away to infinity and

destabilize a compactification, the potential for the runaway moduli generally depends on them.

Solving the scalar equation of motion at a local minimum $V(\phi_*)$ yields a cosmological constant $\Lambda_* = V_*/M_P^2$. The classical solution for the metric is then de Sitter space for $V_* > 0$, Minkowski space for $V_* = 0$, and anti-de Sitter space for $V_* < 0$. The global structures of these three spaces are quite different, so a small positive value is qualitatively distinct from a precisely zero energy vacuum or a small negative one.

The simplest two possibilities are indicated in figures 1-2. In figure 1, one obtains an AdS solution in expansion about weak coupling by playing a negative contribution off of a positive contribution at higher order. In figure 2, one obtains a dS solution by playing a leading order positive contribution off of a subleading negative and a further subleading positive contribution. In all cases, a necessary condition for control is that the coefficients of the subleading terms be >> 1 so that the coupling is stabilized at a weak value.

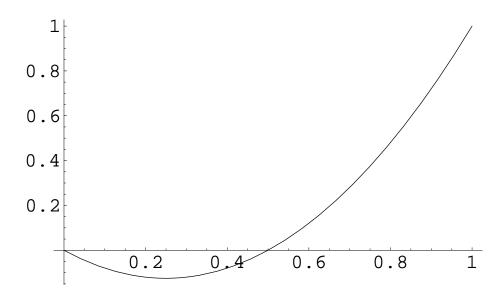


Fig. 1: This figure illustrates the simplest way to stabilize the moduli near weak coupling with a negative cosmological constant. The horizontal axis is the coupling and the vertical is the potential.

By using the known ingredients in string theory, we will find that with $\mathcal{N} \leq 1$ supersymmetry in four dimensions we can find compensating forces on all the moduli, and strong evidence that they can be arranged to yield many vacua with a finely spaced "discretuum" of possible values for V_* . Genericity arguments along the lines of [4] suggest the presence of small nonzero cosmological constant vacua, but don't guarantee (or even suggest) the

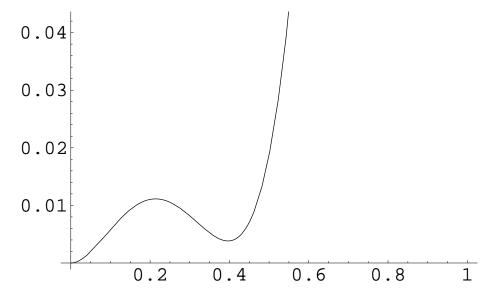


Fig. 2: This figure illustrates the simplest way to stabilize the moduli at positive cosmological constant near weak coupling. At least three independent terms in an expansion about weak coupling are required, with the middle term negative.

presence of vacua with broken supersymmetry and precisely zero cosmological constant in four dimensions.

Another general feature of the moduli potential is that it is extremized at enhanced symmetry points. These are special loci in ϕ space where an extra symmetry appears. Expanding around such a point $\vec{\phi} = \vec{\phi}_* + \delta \vec{\phi}$, where $\vec{\phi}_*$ is the enhanced symmetry point (ESP) and $\delta \vec{\phi}$ transforms nontrivially under the symmetry, one cannot have a term in the potential linear in $\delta \vec{\phi}$. Hence the ESP is at least an extremum of the effective potential in the directions $\delta \vec{\phi}$ acted on by the symmetry. Some of these extrema are local minima, and some are saddle points or local maxima of the effective potential. It was suggested in e.g. [5] that such points may play a special role in string cosmology. Recently, dynamical mechanism trapping kinetic-dominated scalar fields at such ESPs has emerged [6], as have results suggesting a distribution of solutions clustered near certain ESP loci [7].

2.2. Dimensionality and the tree level cosmological term

Let us begin our enumeration of contributions to the cosmological term in string theory with perhaps the most basic contribution. Perturbative string theory can be formulated in any dimensionality, with the "critical dimension" having the property that the classical theory has exactly flat solutions in the prescribed dimension ($D_{crit} = 10$ for the superstring, $D_{crit} = 26$ for the bosonic string).

Since exactly flat spacetime is non-generic and unrealistic, this alone does not argue for the critical dimension. It is possible however, and widely assumed, that supersymmetry provides a reason to specialize to this case. In particular, in the case of string theories with worldsheet supersymmetry, the flat space solution of the critical theory also has extended supersymmetry in spacetime, which reduces on appropriate compactifications to theories with supersymmetric low energy effective actions governing the dynamics in four dimensions. This symmetry provides an elegant solution to the problem of understanding the hierarchy between the Planck and electroweak scales, contributes a natural dark matter candidate, and facilitates the unification of forces into grand unified theories—and therefore is a leading contender for particle physics beyond the Standard Model. However, at this writing it remains an open experimental problem to determine whether supersymmetry plays this role in nature; no direct evidence exists to decide this question. Independently of that, supersymmetry simplifies the analysis of quantum field theory and string theory. It is not known whether or not the noncritical strings have supersymmetric vacua, though as we will discuss below there are some reasons to expect that at least the critical superstring theories arise as vacua of some of the supercritical string theories.

In any case, in order to understand what (if anything) the theory as a whole might predict, and more modestly to understand the full range of known model building possibilities, it is important to consider the string theory vacua in generic dimensions. In D dimensions, one finds a contribution to the tree level dilaton potential of order

$$\Delta \mathcal{V}_s^{(4)} \propto \frac{(D - D_{crit})}{l_s^4} e^{-2\Phi} V_X \tag{2.9}$$

as discussed in [8][9][10]. In four-dimensional Einstein frame, following our derivation (2.8) this is

$$\Delta\Lambda_E \propto \frac{(D - D_{crit})}{l_4^2} \frac{e^{2\Phi}}{V_X} \tag{2.10}$$

This follows from studying the worldsheet reparameterization and Weyl symmetries in the presence of an arbitrary number of free matter scalars X^M , $M=0,\ldots,D-1$; one finds a contribution to the trace of the worldsheet stress-energy tensor proportional to $D-D_{crit}$. Following the discussion in [10], starting from the flat worldsheet metric $\eta_{\alpha\beta}$ we could fix classically, we vary it to $g_{\alpha\beta}=\eta_{\alpha\beta}+h_{\alpha\beta}$, whereupon the worldsheet action changes by

$$\delta S_{ws} = \int d^2 z T_{\alpha\beta} h^{\alpha\beta} \tag{2.11}$$

where $T_{\alpha\beta}$ is the worldsheet stress-energy tensor. After this deformation, the stress energy tensor shifts, in particular

$$\delta < T_{zz} > = < T_{zz} \int h_{\alpha\beta} T^{\alpha\beta} > \sim (D - D_{crit}) \int \frac{h_{\bar{z}\bar{z}}}{z^4}$$
 (2.12)

to leading order in the deformation. Now if at this order $T_{\bar{z}z}$ were still zero, we would lose energy-momentum conservation since

$$\partial^{\alpha} T_{\alpha\beta} = \partial^{z} T_{zz} + \partial^{\bar{z}} T_{\bar{z}z} \tag{2.13}$$

Since the first term here is nonzero, so must be the second term to preserve energymomentum conservation on the string worldsheet. This leads to a covariant contribution

$$T_{\alpha}^{\alpha} = -\frac{(D - D_{crit})}{12} \mathcal{R}^{(2)} \tag{2.14}$$

where $\mathcal{R}^{(2)}$ is the worldsheet curvature scalar. In other words, in a flat spacetime background with constant dilaton, the theory would not preserve Weyl invariance. However, in general there are other contributions, such as that generated by the worldsheet coupling $\int \Phi \mathcal{R}^{(2)}$. Taking this into account, one finds a dilaton equation of motion

$$T_{\alpha}^{\alpha} = -\frac{1}{2} \mathcal{R}^{(2)} \left(\frac{(D - D_{crit})}{6} - \alpha' \nabla^2 \Phi + \alpha' (\nabla \Phi)^2 + \ldots \right)$$
 (2.15)

where the $+ \dots$ refers to higher orders in the α' and string loop expansion and contributions from other fields such as curvatures and fluxes (to be discussed below). The terms in (2.15) arise from a cosmological term of the form (2.10) in the low energy effective action.

One would like to know how these noncritical theories fit into the web of M theory backgrounds. It is likely that they are related by closed string tachyon condensation, related to turning on relevant perturbations on the string worldsheet (see the recent paper [11] for an interesting example of this in some concrete heterotic models). As discussed in [8], worldsheet renormalization group flows are related to spacetime instabilities; condensing tachyons leads to reduction in the worldsheet degrees of freedom in the matter sector. We see that in the above result: condensing a tachyon would reduce the potential energy, which correlates with reducing $D - D_{crit}$. In the next subsection, we will see that positive spacetime curvature has the same effect, so that compactifying the supercritical theories on positively curved spaces such as spheres may reduce them to critical theories.⁴

⁴ J. Polchinski has developed this relation more precisely in some cases.

2.3. Spatial Curvature in the Compactification

Starting from the Einstein term in D dimensions, dimensionally reducing over X produces a contribution to the four-dimensional effective action which scales like

$$\Delta\Lambda_s \sim -\int d^4x \sqrt{g_s^{(4)}} \int_X \mathcal{R}^{(X)} \frac{e^{-2\Phi}}{l_s^8}$$
 (2.16)

in string frame, and correspondingly rescaled as in (2.8) in Einstein frame. The sign here comes from the fact that the gravitational action (2.1) contributes to the *potential* energy term with a minus sign. For example, if we compactify on an S^6 of volume $V_X l_s^6 = L^6 l_s^6$ we obtain

$$\Delta\Lambda_E \sim -\frac{1}{l_4^2} \frac{1}{L^2} \frac{e^{2\Phi}}{V_X} \tag{2.17}$$

in four dimensional Einstein frame, using the fact that the curvature scales like $1/L^2$ and positive curvature contributes negatively to the potential energy term in the Lagrangian. (Note that the conversion to Einstein frame does not act on the internal metric or curvature.) In general, it is worth remarking on the sign: negative curvature contributes positively to the four dimensional potential energy, while positive curvature contributes negatively.

2.4. Fluxes

An important contribution to the moduli potential comes from fluxes on cycles of the compactification (see [12][13][14][15]. for some of the original papers on this method for lifting the moduli in string theory). These are quantized: in terms of a p-form field strength F_p on a p-cycle C_p we get

$$\frac{1}{2\pi l_s^{p-1}} \int_{C_p} F_p = Q_p \tag{2.18}$$

with integer Q_p . This contributes positive potential energy via the flux kinetic terms proportional to $F_p^2 \sim Q^2/(V_p^2 l_s^2)$, where V_p is the volume of the p cycle in string units (i.e. the volume divided by l_s^p). Here we are taking a uniform flux on the p-cycle. For NS fields this kinetic term arises at the closed string tree level, multiplied by $e^{-2\Phi}$ in string frame. RR fluxes have no e^{Φ} factors in front of their kinetic terms in string frame.

We can now calculate the contribution to Λ of the flux kinetic terms in Einstein frame taking into account the results of §2.1. For example, for NS 3-form flux H or RR 3-form

flux F on a compactification from 7 to 4 dimensions on a 3-sphere of volume $V_3l_s^3$ one finds respectively

$$\Delta\Lambda_E \sim \frac{e^{2\Phi}Q_H^2}{l_4^2 V_3^3} \tag{2.19}$$

and

$$\Delta\Lambda_E \sim \frac{e^{4\Phi}Q_F^2}{l_4^2 V_3^3} \tag{2.20}$$

Note that the fluxes naturally force the cycles to expand, lowering the flux energy density on the cycles. Note also that the RR fluxes come at the same order as 1-loop effects.

There are many choices of fluxes on a typical compactification, leading to huge numbers of vacua as discussed first in [4]. We will explain a simple estimate for this number in flux compactifications when we get to the models in §3.

There are important couplings involving F_3 and H_3 which I should note. Firstly, we must take into account axion couplings. In the type IIB Lagrangian in 10 dimensions, we have a term proportional to

$$\int d^{10}x \frac{\sqrt{g_s^{(10)}}}{l_s^8} |F - C_0 H|^2 \tag{2.21}$$

where C_0 is the IIB axion [16]. So although the axion is a periodic variable, not subject to runaway to infinity, its VEV affects the forces on the other moduli including the potential runaway directions such as the dilaton. Also, there is an important topological restriction on compact manifolds coming from a contribution of 3-form fluxes to 3-brane charge: the Gauss' law relation between $L \sim \int H \wedge F$ and orientifold 3-plane and D3-brane charge is

$$\frac{1}{2(2\pi)^4(\alpha')^2} \int H \wedge F = \frac{1}{4} (N_{O3} - N_{\overline{O3}}) - N_{D3} + N_{\overline{D3}}$$
 (2.22)

This contribution to the 3-brane charge from $\int H \wedge F$ comes from a coupling $\int C_4 \wedge F \wedge H$ between the 3-brane gauge potential C_4 and $H \wedge F$. In the next section we will study the contribution of branes to the moduli potential.

2.5. Orientifolds and D-branes

Next let us turn to the effects of defects in the compactification. In particular, Dpbranes and orientifolds contribute to the low energy effective potential via their tension. From their string frame tension [9][16], $T_{Dp,s} \sim \frac{1}{g_s l_s^{p+1}}$, a Dp-brane at a point in a compactification on X with volume V_X in string units produces a 4d Einstein frame potential energy

$$\Delta\Lambda_E \sim \frac{e^{3\Phi}}{l_4^2 V_X^2} \tag{2.23}$$

Similarly, orientifold planes make a contribution scaling the same parameterically as a function of the coupling and volume, but with an opposite sign.⁵ This negative contribution from orientifolds will be crucial, and makes sense physically because orientifolds involve a Z_2 identification which changes the asymptotic geometry far from the object–hence they cannot be dynamically produced. Relatedly, their number in any given compactification is bounded. This places interesting limitations on stabilization of moduli, since the strength of the negative contribution to the potential in figure 2 is important for determining how small the cosmological constant can be.

As observed and used in [17], in the presence of warping in a compactification, defects localized in regions of small warp factor have an extra suppression to their tension. This provides a natural way in which these objects can provide forces competing with contributions which are a priori more subleading, such as perturbative and non-perturbative quantum corrections.

2.6. Loop Effects

Although they appeared at different orders in $g_s \sim e^{\Phi}$, the contributions we discussed so far are all classical energy densities. Quantum corrections also generically arise and can compete with the other effects.

At one loop in perturbation theory, in the presence of $\mathcal{N}=1$ or $\mathcal{N}=0$ supersymmetry, the moduli potential receives corrections. The computation of the 1-loop potential is discussed in detail in [9] (chapter 7), whose description I largely worked through in the lectures at the schools but will not reproduce here. The result is UV sensitive, generalizing the field theory result $\Lambda_{1-loop}=\int \frac{d^3\vec{k}}{(2\pi)^3}\omega_{\vec{k}}$ where $\omega_{\vec{k}}$ is the frequency of the mode solutions. As discussed above, in flux models the RR fluxes arise at the same order as this 1-loop term, and can be used to tune the total contribution close to a desired value.

⁵ In general dimensions, we can study how the tension of orientifold planes depends on the dimensionality D as well. This was done in [15], where we found that in a toroidal orientifold, the total contribution from the order 2^D orientifold fixed planes scales like $2^{D/4}$.

2.7. Non-Perturbative Effects

In addition to the perturbative contributions, one has non-perturbative corrections coming from instantons, gaugino condensation, and other effects. At the level of a superpotential in models with a supersymmetric low energy effective field theory, such effects can be the leading ones lifting some of the moduli. Many string theories reduce at low energies to the quantum field theories containing the field content producing instantons or gaugino condensation (with the obvious caveat that non-perturbative effects from strong coupling gauge dynamics occurs only in cases with asymptotically free matter content). There have been several good lecture series on this subject, which I will not cover in any detail here (see e.g. [18]). The moduli dependence of such effects comes in part from the gauge theory relation $\Lambda_{QCD} \sim e^{-C/g_{YM}^2}$ where C is an order 1 constant and g_{YM}^2 can depend on volumes of cycles as well as the string coupling. For example, 7-branes wrapped on 4-cycles of linear size Ll_s have $g_{YM}^2 \sim g_s/L^4$.

Nonperturbative effects play an important role in the KKLT construction, to be overviewed in the next section. Specific examples in this context were recently studied in [19].

Also at the classical level, one can have worldsheet instantons which produce corrections non-perturbative in α' [20].

2.8. Tachyons

In addition to tadpole forces on the moduli, one often encounters a situation with a scalar field T in the string theory spectrum whose mass squared is negative. This indicates an instability. In quantum field theory, in this situation one would calmly shift the VEV of T until it reached a metastable vacuum, if one exists in the theory; otherwise one would discard the theory. In perturbative string theory, at the string scale, one is usually stuck with a first quantized description of the unstable maximum, and we generally lack a sufficiently global view of the space of string vacua to determine immediately if T may be shifted away from the unstable maximum at T=0 to a metastable position.

The worldsheet point of view on tachyon condensation is instructive. An on-shell tachyon state is a solution to the worldsheet constraint $L_0|\Psi>=0$ producing the mass shell condition with $k^2=m_T^2<0$. Turning it on at zero momentum k=0 would correspond to a relevant perturbation on the string worldsheet, which results in a decrease in the number of degrees of freedom.

In recent years progress was made on this question for tachyons associated to D-branes (covered in Sen's lectures), and localized tachyons in the twisted closed string spectrum of orbifold theories. For example [21], consider orbifolds of the type II string in which we make a Z_k identification with generator

$$g: \quad z_j \to e^{2\pi n_j i/k} z_j \tag{2.24}$$

on complex coordinates z_j , $j=1,\ldots,d/2$ for some integers n_j . This produces a cone, with tip at $z_j=0$ and a base S^{d-1}/Z_k determined by the action (2.24) on the angular directions in $\mathbb{C}^{d/2}$. The spectrum of closed strings includes those twisted by $g^n, n=1,\ldots,k-1$. That is, in the *nth* twisted sector, the worldsheet scalars $Z_j(\sigma,\tau)$ corresponding to the spacetime coordinates z_j satisfy

$$Z_j(\sigma + 2\pi, \tau) = g^n Z_j(\sigma) \tag{2.25}$$

with the spacetime fermions satisfying corresponding relations. This twisting of the boundary conditions of the closed string leads to a modification of the ground state energy in the twisted sectors, and generically one finds tachyons in the twisted sectors.

The tip of the cone is a highly curved region, for which low energy field theory and general relativity are not sufficient. This is one of the simplest examples of a naked singularity which is resolved by string theory, at least in the cases where the deficit angles in the cone are orbifold angles. In these situations, D-brane probes can be used to determine the leading effect of condensing T; as described in [21], this leads to decay into $Z_{k'}$ orbifolds for k' < k and matches to solutions in which a shell of graviton-dilaton solution interpolates between the $Z_{k'}$ conical tip and the $\mathbb{R} \times S^{d/2}/\mathbb{Z}_k$ asymptotics (as studied in [21][22]). Other techniques use the power of worldsheet supersymmetry to control the RG flow for the lowest tachyons in these models [23]. In addition, one can regulate the situation with an extra shift, producing examples amenable to a low energy field theory analysis [24]. Finally string field theory has been successfully applied to this process in [25].

It is still an open question to determine the fate of bulk (as opposed to localized) tachyons. Some interesting ideas were proposed recently in [26][24][27]. The proposal in [27] that RR flux can stabilize closed string tachyons is intruiging. However in AdS/CFT examples with tachyons from orbifolds (such as the type 0 theory) one finds a remaining Coleman-Weinberg instability at small radius (where the RR flux energy density is large and could in principle have removed the instability). The instability takes the system to a new vacuum with fewer degrees of freedom, as expected from the worldsheet RG picture of tachyon condensation, reducing the system to pure Yang-Mills theory at low energies [28][29].

2.9. Orbifolding to fix moduli

Another useful technique to fix moduli is orbifolding. As discussed in the simple example in the last subsection, an orbifold projects out states which are not invariant under the orbifold action. This can eliminate moduli and tachyons. However it also entails the addition of the twisted sectors, which can reintroduce moduli and tachyons.

A particularly useful technique for eliminating moduli is asymmetric orbifolding [30]. This can be viewed as modding out by T-duality. For example, let us consider the T-duality action which inverts the volume of a product of circles. For each S^1 , at a generic radius this T-duality action maps one model into another, but at the self-dual radius T-duality fixes the background. At this radius, one has zero mode worldsheet momenta

$$\alpha_0 = \frac{(n+w)}{\sqrt{\alpha'}}$$
 $\tilde{\alpha}_0 = \frac{(n-w)}{\sqrt{\alpha'}}$ (2.26)

in terms of momentum and winding quantum numbers n and w. T-duality acts by taking $\alpha \to -\alpha, \tilde{\alpha} \to \tilde{\alpha}$, or in other words $X_L \to -X_L, X_R \to -X_R$ where X_L and X_R are the left and right moving worldsheet scalars corresponding to the circle direction in the target spacetime. It leaves the spectrum invariant, as seen by exchanging $n \leftrightarrow w$.

This action has the great virtue of removing the untwisted moduli, since it acts on the corresponding vertex operators as

$$T: (V \sim \partial X_L^M \bar{\partial} X_R^N) \to -V$$
 (2.27)

It is not quite as easy as this makes it sound: there are important constraints on such models, encoded by modular invariance, and as mentioned above the twisted sectors can reintroduce moduli (and/or tachyons in some cases). Solutions to all these constraints preserving the beneficial effects of (2.27) have been studied in [15], which we will explore more fully below.

Note that this asymmetric orbifold action is non-geometrical, and one can (and should) explore further generalizations of string compactifications to include non-geometrical ones, as done for example in the recent works [31]. In any case, the ingredients and techniques we have covered here so far will suffice to provide interesting models with compensating forces on all the moduli.

3. Models of Moduli Stabilization

Using the ingredients catalogued in §2, it is straightforward to arrange them to provide compensating forces on the moduli. In this section we will study three illustrative cases. For each, we put together appropriate combinations of the terms and techniques discussed above, and explain the origin of the large numbers required to obtain a solution expanding around weak coupling or large radius. The second case here is new and raises some interesting questions. The third case is the dS models [15][17]. There have been many other interesting papers on how to stabilize moduli in other classes of models [32][33].

3.1. Compactification on S^5

Let us warm up by discussing the compactification of type IIB string theory on S^5 . This is probably familiar to you in your studies of the AdS/CFT correspondence, where the corresponding solution is usually presented in its full ten-dimensional glory. Here we will simply recover the AdS_5 solution using the five-dimensional low energy effective theory description analogous to that developed in the previous section for the four-dimensional case. This provides a useful check on our understanding, and gives a method which generalizes to the cases of interest such as compactification on Calabi-Yau manifolds, where a full 10d geometry is not known but the low energy effective field theory is sufficient to determine the low energy potential for the moduli. (In fact, we will find in this subsection that the S^5 is stabilized at the same radius as that of the AdS, which means the Kaluza-Klein modes need to be included in studying the dynamics of the model.)

Compactifying on an S^5 with radius Ll_s produces a negative contribution to the 5d cosmological term from the positive curvature of the S^5 . In string frame, this is

$$\Lambda_{\mathcal{R}}^{(s)} \sim -\frac{L^5}{e^{2\Phi}} \frac{1}{L^2 l_s^2}$$
(3.1)

using the fact that the curvature scales like $1/(L^2l_s^2)$, appears at tree level in the g_s expansion, and is integrated over the whole S^5 . In the *five*-dimensional Einstein frame, this becomes

$$\Lambda_{\mathcal{R}}^{(E)} \sim -\frac{e^{\frac{4}{3}\Phi}}{l_5^2 L^{16/3}}$$
(3.2)

As it must, this contribution goes to zero as the radius L of the S^5 goes to infinity.

As it stands, this contribution alone would drive the system toward higher curvature (a big crunch in the S^5 directions). However we can provide a compensating force using the

five form flux of the IIB theory. Putting N units of this flux on the S^5 (and correspondingly on the remaining 5 directions by the self-duality of the flux in IIB), we obtain a second contribution to the 5d effective theory's potential energy. This is in string frame

$$\Lambda_F^{(s)} \sim \frac{L^5}{l_s^2} \frac{N^2}{L^{10}} \tag{3.3}$$

and in Einstein frame

$$\Lambda_F^{(E)} \sim \frac{N^2}{l_5^2} \frac{e^{10\Phi/3}}{L^{40/3}}$$
(3.4)

For $L \to 0$, the flux term dominates while for $L \to \infty$, the curvature term dominates. If we choose a sufficiently large coefficient N, we can arrange that the two balance at a value of L which is large enough that this low energy effective field theory analysis (using supergravity alone rather than the full string theory) applies. At the minimum, the 5d cosmological constant is negative, producing an AdS_5 solution. To simplify the picture let us define a variable

$$\eta \equiv \frac{e^{\Phi/3}}{L^{4/3}} \tag{3.5}$$

In terms of η , the form of the potential is

$$\Lambda_E(\eta) = -\eta^4 + N^2 \eta^{10} \tag{3.6}$$

At the minimum, this satisfies

$$\eta_*^6 \propto \frac{1}{N^2} \tag{3.7}$$

From our definition of η (3.5), we can rewrite this in terms of the original variables as $\frac{L^8}{g_s^2} \sim N^2$, i.e. the familiar result $L \sim (g_s N)^{1/4}$. So far this reproduces the expected radius of the S^5 (and the fact that there is a family of solutions obtained by varying g_s). What about the curvature radius of the AdS_5 ? In our 5d effective field theory description, this is determined by the value of the cosmological constant at the minimum. This is

$$\Lambda_{min} \sim -\frac{1}{l_5^2} \frac{g_s^{4/3}}{L^{10/3}} \frac{1}{L^2} \tag{3.8}$$

Now using the fact that the 5d Planck length l_5 is determined by $l_5^3 = g_s^2 l_s^3/L^5$, or $l_5^2 = g_s^{4/3} l_s^2/L^{10/3}$, we obtain from (3.8) that

$$\Lambda_{min} \sim \frac{1}{L^2 l_s^2} \tag{3.9}$$

So the curvature radius of the AdS_5 is indeed Ll_s .

3.2. Type IIB on $S^3 \times S^3$ With Flux

Next let me mention a new example, which shares some features with the one we just considered as well as with the $(A)dS_4$ flux compactifications we will consider later.⁶ Consider type IIB string theory compactified on $S^3 \times S^3$, putting Q_1, Q_2 units of RR 3-form flux $\int F$ on the first and second S^3 factors respectively, and similarly N_1, N_2 units of NS 3-form flux $\int H$. In fact, for simplicity let us take $|N_1| = |N_2| \equiv N$ and $|Q_1| = |Q_2| \equiv Q$, with the signs determined by a simplifying assumption of cancelling the axion tadpole in (2.21).

Using the methods developed in §2, we will solve the equations of motion for the dilaton and the radii R_1l_s , R_2l_s of the two 3-spheres (with a round metric for simplicity). First we must take into account the effects of the F and H flux on other degrees of freedom of the system, as discussed in §2.4. In particular, we can choose the F and H flux to cancel the axion tadpole in (2.21). This leaves us with of order QN anti-D3-branes needed to cancel $\int H \wedge F$ contribution to Gauss' law (2.22).

Now from our considerations in §2, we can write the structure of the cosmological term in this model:

$$\Lambda_{E} = \frac{1}{l_{4}^{2}} \frac{e^{4\Phi}}{R_{1}^{6} R_{2}^{6}} \left(-\frac{R_{1}^{3} R_{2}^{3}}{R_{1}^{2}} e^{-2\Phi} - \frac{R_{1}^{3} R_{2}^{3}}{R_{2}^{2}} e^{-2\Phi} + \frac{N_{1}^{2} R_{2}^{3}}{R_{1}^{3}} e^{-2\Phi} + \frac{N_{2}^{2} R_{1}^{3}}{R_{2}^{3}} e^{-2\Phi} + \frac{\tilde{N}_{2}^{2} R_{1}^{3}}{R_{2}^{3}} e^{-2\Phi} + \tilde{N}_{2}^{2} R_{2}^{3} e^{-2\Phi} + \tilde{N}_{2}^{2} R_{2}^{2} e^{-2\Phi} + \tilde{N}_{2}^{2}$$

The first two terms here come from the positive curvature of the S^3 s. The next two come from the NS H flux. The next term (with order one coefficient \tilde{c}) is the contribution of the order QN anti-D3-branes. Finally, the last two terms are the contributions of the RR fluxes. The symmetries of the round sphere metric imply that the equations of motion are automatically solved for the non-radial moduli of the 3-sphere metrics.

It is straightforward to solve $\partial \Lambda/\partial \Phi = \partial \Lambda/\partial R_1 = \partial \Lambda/\partial R_2 = 0$. The result is parameterically $e^{\Phi} \sim N/Q$ and $R_1 = R_2 \sim N^{1/2}$ in the solution.

Having solved the equations of motion for the moduli, the next step would be to check for tachyons in the diagonalized mass matrix of R_1, R_2, Φ , as well as the axions and higher KK modes in this space. As far as the zero mode moduli go, the potential (3.10) is of the shape in figure 1 in each direction. However, as shown in [34], the low lying Kaluza

⁶ I thank S. Hellerman for very useful discussions on this construction, in particular for alerting me to an important constraint coming from the IIB axion.

Klein modes can sometimes become tachyonic. I have not completed this calculation, but it would be interesting to do so along the lines of [34]; our setup is somewhat different because we do not have a 6-form flux on the compactification, but rather individual 3-form fluxes.

In the next section, we will review among other things the KKLT models with NS and RR flux on 3-cycles of Calabi-Yau compactifications [17]. The model in this subsection may be a good toy model for some aspects of [17], since it involves fluxes on dual three-cycles. In the $S^3 \times S^3$ case, the system might arise via a finely tuned near horizon limit of D5 and NS5 branes wrapping 3-cycles in the base of a cone over $S^3 \times S^3$. However, this model, like the $AdS_5 \times S^5$ model, has an AdS curvature radius of the same order as the radii of the S^3 s. One can avoid this by orbifolding the sphere(s) by a large group [35][36], reducing their volume relative to that of the AdS factor or by compactifying on more complicated spaces and using the three independent terms depicted in figure 2 to stabilize the moduli. It is to this that we will turn next.

3.3. (A)dS Flux Compactifications

We can now put together our ingredients to stabilize the moduli in more complicated compactifications, such as realistic ones down to four dimensions with positive vacuum energy, in which the internal compactification can be parameterically smaller than the curvature radius of the remaining dimensions. I will start by explaining how the dilaton is stabilized in all known examples, and then discuss how the volume and other moduli are addressed in the current proposals.

As far as the dilaton goes, we can write its potential in the general form

$$\Lambda_E = \frac{e^{2\Phi}}{l_4^2} (a - be^{\Phi} + ce^{2\Phi} + \dots)$$
 (3.11)

where the $+\dots$ refers to terms subleading and non-perturbative in the expansion around small $g_s = e^{\Phi}$. Here the coefficients a, b, and c can come from the following sources from our list developed above. First, the coefficient a arises at closed string tree level, and so could get contributions from dimensionality ($D \neq D_{crit}$), curvature, and NS flux H^2 for example. The b coefficient comes from orientifolds and D-branes, while the c coefficient comes from RR flux F^2 and the 1-loop correction to the cosmological term.

As far as the quantum contribution to the c coefficient, it is useful to use the Bousso-Polchinski prescription [4] to arrange the RR fluxes to dominate over the 1-loop cosmological term and tune the sum to close to a desired value. In order to calculate precisely the

fluxes involved in a given model, it would be necessary to compute this contribution and specify the fluxes required to make such a tune.

In order to stabilize the dilaton at a negative vacuum energy, we can play off a leading order negative term against a subleading positive term (with a large coefficient to obtain control). For example, one could consider a subcritical dimensionality (or positive curvature) to obtain a negative tree-level cosmological term, balanced against a positive contribution from D-branes or RR flux. (We saw one version of this in the last subsection.)

By allowing all three terms in (3.11) to play a role, we can produce an interesting "discretuum" of (A)dS solutions: the cosmological constant is discretely variable by varying the dimensionality and the brane and flux quantum numbers appearing in a, b, and c.

For example, we can consider a supercritical dimension D, orientifolds, and RR fluxes Q_i on the cycles of a compactification [15]. This yields a metastable minimum at which the positive a term, negative b term, and positive c term balance. For supercritical dimensions, a toroidal orientifold yields a total contribution from the orientifolds which scales like $2^{D/4}$, providing a way, by mildly increasing the dimensionality, to produce a b coefficient in (3.11) parameterically larger than the a coefficient. One has of order 2^D RR fluxes to choose from, allowing a Bousso-Polchinski tuning mechanism.

The bare string coupling is fixed in the metastable minimum of (3.11) at order $2^{-D/4}$. However, there are many species of fields in a generic model of this sort—of order 2^D RR fields can propagate in loops in diagrams. On the other hand, as a function of dimension loop momentum integrals are suppressed by powers of $1/\Gamma(D/2)$ as explored in [37]. It is an open issue to determine the true expansion parameter in the model and ensure that the calculations are under control. This is a general issue in any model once all moduli become fixed—it is no longer possible to tune the coupling below any desired value holding other quantities fixed, and there is always a danger that the true expansion parameter is out of control.

In this model, one can fix all the other NS moduli such as the overall volume via an asymmetric orbifold [15]. As discussed above, there are important constraints from modular invariance on asymmetric orbifolding, which for example allow for the standard GSO projection only in certain dimensions. However the problem of avoiding twisted tachyons and moduli becomes easier in higher dimensions, since twist operators in the orbifold CFT have higher dimensions as we scale up the dimensionality of the target space acted on by the group.

Within the critical string theory, one can similarly fix the dilaton (as well as complex structure moduli of Calabi-Yau compactifications) via a similar balance of forces [14]. In this case, to obtain a positive a coefficient in (3.11), one includes NS flux H^2 . Again one considers orientifold 3-planes and RR fluxes to make up the negative b and positive c terms in (3.11). This setup has been developed very elegantly using the supersymmetric effective field theory packaging into superpotential and Kahler potential terms in [13][14]. Since this has been covered elsewhere, we will here confine ourselves to the component description developed in these lectures.

In this framework, one can further fix the Kahler moduli by including non-perturbative effects [17]. In particular, there are many models with non-perturbative contributions to the superpotential, scaling like $e^{-c_{np}L_{cy}^4/g_s}$ from gauge theory effects on 7-branes wrapped on 4-cycles (where L_{cy} is the length scale of the Calabi-Yau in string units, taken isotropic for simplicity). For example, given a gauge theory with no massless flavors in four dimensions, coming from wrapped 7-branes, one obtains a gaugino condensation-induced superpotential. In the presence of a generic superpotential, one finds AdS_4 solutions preserving supersymmetry. Adding an anti-D3-brane [17][38][39], or starting from a higher energy metastable vacuum of the flux superpotential [40], produces an independent positive contribution to the potential for the volume modulus which can dominate at large L_{CY} and play off the non-perturbative effects, producing very plausibly de Sitter metastable minima of the potential. In this case, the large numbers introduced include flux quantum numbers, and relatedly warping of the compactification which allows the antibrane to contributed a naturally small contribution to the potential which can play off against non-perturbative effects.

Again, once all moduli are fixed the question remains of the expansion parameters involved near large radius and weak coupling. As before, the existence of forces playing off each other with the right relative signs to produce metastable minima, combined with the large number of flux choices available, strongly suggests by genericity that (A)dS minima obtained by these arguments are available as solutions of the full system. Nonetheless, it would be useful to produce completely explicit examples in which all relevant effects are computed, and in which the expansion parameter is determined, at least near the order in which one works, via explicit computations of the next to leading order effects.

The framework [15] is currently more amenable to a worldsheet string theory analysis, as all contributions involved in fixing the moduli are perturbative, while the framework [17] is currently more closely tied to well understood supersymmetric backgrounds of M theory,

and is the only existing proposal with low energy supersymmetry built in, potentially a phenomenologically important feature. Given the genericity of a nontrivial potential energy with multiple minima in low energy effective field theory, it seems likely that there are many classes of models, including ones starting from other limits of the theory such as the heterotic string [33].

One application of these models is to phenomenology. One aspect of this is the question of understanding the distribution of masses and couplings available in low energy limits of string theory. Another aspect is the use of the specific features of this space of string vacua for model-building, without attempting to obtain a general prediction of string theory from the whole set.

Another application is to the physics of inflation, and dark energy. On the latter subject, one would in particular like to know the form of holography in four dimensional AdS (and possibly dS) backgrounds. It is to this that we will turn in the next section. First we provide an intuitive argument for the number of vacua expected from this sort of construction.

3.4. Number of vacua

The Bousso Polchinski mechanism predicts exponentially many vacua as a function of multiple input flux quantum numbers, as follows [4][41][42][43]. The basic idea is the following. One expects a limit on the strength of flux quantum numbers from back reaction on the geometry. Let us consider for example the KKLT case [17]. There are b_3 RR flux quantum numbers Q_i , $i = 1, ..., b_3$ and b_3 NS flux quantum numbers N_i , $i = 1, ..., b_3$. If one expresses the expected limitation in the form

$$R^2 \equiv \sum_{i=1}^{b_3} \gamma_i Q_i^2 + \alpha_i N_i^2 < R_{max}^2$$
 (3.12)

for some order one coefficients α_i and γ_i , then one obtains a total number of vacua which is of order

$$N_{vac} \sim \frac{R_{max}^{2b_3}}{b_3!} \tag{3.13}$$

from the volume of the sphere in flux space containing the fluxes consistent with (3.12). (This assumes that each choice of flux leads to of order one vacua.)

In the KKLT models, this estimate may be given in terms of the quadratic form

$$Q \odot N \sim \int_{CY} H \wedge F \tag{3.14}$$

as follows. Dimensional reduction on a space with flux produces contributions to the four dimensional effective potential from the flux kinetic terms for the NS flux H_{NS} and the Ramond flux F_{RR}

$$\Lambda_{flux} \sim \int_{CY} \frac{1}{l_4^2} \frac{e^{4\Phi}}{V^2} \sqrt{g} (|F_{RR}|^2 + e^{-2\Phi} |H_{NS}|^2). \tag{3.15}$$

where we are in 4d Einstein frame and V is the compactification volume in string units. This contribution takes the form

$$\Lambda_{flux} \sim \sum_{i=1}^{b_3} (c_i Q_i^2 + a_i N_i^2)$$
 (3.16)

where a_i and c_i are functions of the moduli, which in turn depend on the fluxes, and Q_i and N_i are the RR and NSNS flux quantum numbers on the 3-cycles in the compactification. (In asymmetric orbifold models such as [15] the dependence of a_i , c_i on the moduli is eliminated for the geometrical moduli by using asymmetric orbifolding to freeze them at the string scale.)

If we pick the maximum flux scale R_{max} such that the moduli-dependent coefficients a_i and c_i do not take extreme values in the solutions to the equations of motion, then one can relate $Q \odot N$ to a positive definite quadratic form for each point on the moduli space solving the equations of motion.

That is, in the no scale models [44] appearing in KKLT, the Gauss' law relation between $\int H \wedge F$ and orientifold 3-plane and D3-brane charge

$$\frac{1}{2(2\pi)^4(\alpha')^2} \int H \wedge F = \frac{1}{4} (N_{O3} - N_{\overline{O3}}) - N_{D3} + N_{\overline{D3}}$$
 (3.17)

translates via supersymmetry into a relation between the orientifold +D3-brane tension and $Q \odot N$. In a zero energy vacuum of the no-scale approximation [44] to the effective potential, this tension $\int H \wedge F$ cancels the positive terms (3.16) in the potential. So for every solution to the equations of motion we wish to consider, a relation of the form

$$\sum a_i N_i^2 + c_i Q_i^2 \sim Q \odot N \le R_{max}^2 \tag{3.18}$$

holds, with a_i and c_i order one coefficients that depend on the fluxes. So rewriting R_{max}^2 as $Q \odot N_{max}$ we can rewrite (3.13) as

$$N_{vac} \sim \frac{(Q \odot N)_{max}^{b_3}}{b_3!} \tag{3.19}$$

By integrating the number of vacua solving the equations of motion over the flux choices and moduli space with a suppression factor introduced for large fluxes to take into account (3.18), [43] found an estimate

$$N_{vac} \sim \frac{(2\pi(Q \odot N)_{max})^{b_3}}{b_3!} f(b_3)$$
 (3.20)

Here $f(b_3)$ is an integral of flux-independent quantities over a fundamental domain of the moduli space.

This estimate, which may ultimately prove accurate as a count of the number of IIB flux vacua, appears at least to be a lower bound on this number. There are other classes of vacua such as [15] to be included in a full count as well, though the corresponding entropies for these may be studied independently.

4. The Coulomb Branch and Entropy

In both the AdS and dS case, one expects an entropy associated to the solutions, scaling like

$$S \sim \frac{1}{l_4^2 \Lambda} \tag{4.1}$$

where Λ is the Einstein-frame cosmological constant in the (meta-)stable minimum and l_4 is the four-dimensional Planck length. In the AdS case, this arises from a trivial application of the Susskind-Witten arguments from AdS/CFT [45] to this case, and in the dS case follows from old arguments of Gibbons and Hawking [46]. As in black hole physics, this suggests a microphysical count of states, and perhaps a broader holographic relation. In this section, I will explain recent progress in extracting these microphysical degrees of freedom in the flux compactifications to four dimensions.⁷

Before proceeding, let me dispel a potential confusion. The AdS/CFT duality was argued initially based on near horizon limits of D-brane systems [48]. In most solutions, even most AdS solutions, such as those developed in these notes, the solutions are not realized in this way. The argument based on a near horizon limit involves extending the system to one with infinitely more degrees of freedom, and then scaling them out to obtain the precise equivalence discovered in this way by Maldacena [48]. The AdS/CFT dictionary subsequently articulated in [49] makes no reference to the non-near horizon

⁷ Other approaches to de Sitter holography were reviewed recently in [47].

geometry forming the starting point of the argument [48], and indeed the equivalence between AdS string theory and CFT requires no such extension in general. This strongly motivates proceeding to seek a dual description of the $(A)dS_4$ flux models, but raises at the same time the question of how to extract the dual description in the absence of a near horizon argument.

One concrete strategy which works is the following. In ordinary AdS/CFT, if one considers the system on its Coulomb branch, the gravity side description of the system includes brane domain walls at positions in the radial direction of the geometry which correspond to the scale of the VEVs turned on in the field theory description. In this configuration, the degrees of freedom of the system (e.g. the N^2 degrees of freedom of the $\mathcal{N}=4$ SYM theory dual to $AdS_5\times S^5$) become manifest on the D-brane domain walls. This allows one to view the microphysical degrees of freedom comprising the entropy without ever needing to extend the system to the non-near-horizon geometry, and without needing to know in advance the field content of the CFT dual.

This procedure is equally well available also in the $(A)dS_4$ flux models. For example, in the KKLT geometry [17], the brane domain walls are D5-branes wrapped on cycles dual to those containing the corresponding RR 3-form flux and NS5-branes wrapped on cycles dual to those containing the corresponding NS 3-form flux. If the pulled-out branes change $\int H \wedge F$, then there must also be a corresponding number of D3-branes ending on the domain walls, to satisfy Gauss' law in the compactification for all radial intervals in (A)dS. This configuration of intersecting 5-branes with 3-branes ending on them is a generalization of the Hanany-Witten setup [50] for studying 3-dimensional gauge theories; our generalization involves live fivebranes (by which I mean that the degrees of freedom of the 5-branes themselves are dynamical, whereas in the original Hanany-Witten setup the fivebranes were of infinite extent and produced non-dynamical couplings). It is worth remarking that in both AdS_4 and dS_4 flux models, these domain walls are generically time dependent solutions rather than static configurations.

In [42], the geometry and causal structure of the Coulomb branch domain wall configurations was determined for the dS case. In [51], the degrees of freedom of the system on the Coulomb branch were identified and shown to agree with the gravity side prediction, as we review below. In [52], it was noted that in the de Sitter case, the system has a "localized graviton" in addition to the horizon entropy; this makes the dS case analogous not to pure AdS/CFT but to the AdS/CFT description of a CFT coupled to gravity.

The opposite extreme to string scale geometries is the case where the (A)dS geometry has a curvature radius tuned to a large value by a generalization of the Bousso-Polchinski mechanism to the flux compactifications. For these examples, the entropy is predicted to be able to be enormous, in the following way. In the above subsection, we found that the number of vacua scales like $N_{vac} \sim \frac{(2\pi(Q \odot N)_{max})^{b_3}}{b_3!} f(b_3)$ (3.20).

If we take these vacua (3.20) to be distributed roughly uniformly between cosmological constants of $\pm \frac{1}{l_4^2}$ (where l_4 is the four-dimensional Planck length), this predicts a minimum cosmological constant of magnitude

$$\Lambda_{min} \sim \frac{1}{l_4^2 N_{vac}} \tag{4.2}$$

corresponding to a maximum curvature radius $L_{(A)dS}$ of order

$$(L_{(A)dS}^{max})^2 \sim l_4^2 N_{vac} \tag{4.3}$$

among the elements of the discretuum of vacua predicted by the estimate (3.19)(3.20). This curvature scale in turn corresponds to an entropy of order

$$S_{max} \sim \frac{((Q \odot N)_{(A)dS}^{max})^2}{l_A^2} \sim N_{vac}$$
 (4.4)

Taking the vacua to be uniformly distributed is a nontrivial assumption, since the vacua could instead accumulate around some particular values of the cosmological constant. We will see that this naive assumption fits with what we find for the entropy, though a much more thorough analysis of the distribution of vacua will ultimately be required.

So from the gravity solution, we obtain a prediction for a large entropy, scaling like

$$S_{max} \sim \frac{(Q \odot N)_{max}^{b_3}}{b_2!}$$
 (4.5)

As discussed in [51], we can obtain this counting via the degrees of freedom evident on the Coulomb branch of the solution, by studying the degrees of freedom living on the brane domain walls described above. For example, we can consider the case where all the (p,q) branes are either D5-branes or NS5-branes (let us say, D5-branes on all the A-cycles of the Calabi-Yau, and NS5-branes on all the B-cycles), with about the same number of each.

We have a gauge group $\prod_{i=1}^{b_3} U(N_i) \times U(Q_i) \times U(N_iQ_i)$ from the NS, D5, and D3-branes respectively. From (3.18) we see that if we distribute the branes uniformly over

the cycles, then $N_i \sim Q_i \sim \sqrt{Q \odot N/b_3}$. We then have $b_3/2$ bunches of D_5 branes, each bunch containing of order $\sqrt{Q \odot N/b_3}$ branes. Similarly we have $b_3/2$ bunches of wrapped NS5-branes, each bunch containing of order $\sqrt{Q \odot N/b_3}$ branes. Finally we have $b_3/2$ bunches of D3-branes stretching from the $b_3/2$ sets of intersecting A and B cycles, each bunch containing of order $Q \odot N/b_3$ branes.

The degrees of freedom living on the branes consist of string junctions and webs. If we consider those ending once on each bunch of branes, they can be electrically charged under each of the U(n) factors in the gauge group. This gives them a chance to survive as we go back to the origin of the approximate Coulomb branch, unlike the (p,q) junctions describing the monopoles and dyons of the $\mathcal{N}=4$ SYM in the $AdS_5 \times S^5$ case. On the other hand, although our counting will work and makes sense from this point of view, we will not be able to establish for certain the stability of these degrees of freedom as we go back to the origin.

Counting these junctions, we obtain a maximum entropy

$$S_{max} \sim \left(\sqrt{\frac{Q \odot N}{b_3}}\right)^{b_3/2} \times \left(\sqrt{\frac{Q \odot N}{b_3}}\right)^{b_3/2} \times \left(\frac{Q \odot N}{b_3}\right)^{b_3/2} \sim \left(\frac{Q \odot N}{b_3}\right)^{b_3}$$
 (4.6) as predicted in (4.5).

There are many interesting open questions to pursue in this direction. For example, we would like to understand in which precise vacua the junction states are stable as one goes back to the origin. This is related to the corresponding question on the gravity side—in which precise flux vacua does the tuning providing a small cosmological constant arise.

More importantly, we would like to understand the form that holography takes in the (A)dS flux vacua, building from our nascent understanding of these vacua and their entropy. The procedure of going on the Coulomb branch, either to a generic Coulomb branch configuration or via a single brane probe, provides a way to study not just the microphysical entropy but also some aspects of the dynamics of the putative dual theory—it is an area of active research. The form holography might take in dS is a conceptually challenging subject (see e.g. [52][53] for some general discussion of issues involved). The holographic relation in this case may not be an exact equivalence to an ordinary non-gravitational system in one lower dimension. However, even at an approximate level (perhaps at times shorter than the decay time out of a given vacuum) it would be very interesting to determine the way the degrees of freedom making up the entropy (4.5)(4.6) account for other aspects of the physics of the system.

More generally, the dynamics on the moduli space of interacting scalar field theory has some important novelties, related to the above issues and to cosmology with scalar field theory. Let us now turn to this subject.

5. Velocity Dependent Effects on Moduli Dynamics

In the preceding sections, I focused on the physics of the scalar potential. It has become increasingly clear that the dynamics of scalar fields is significantly affected also by kinetic effects. Therefore for completeness I will summarize in this section recent developments involving these effects [54][6] (closely related to earlier developments in the subject of reheating after inflation [55], earlier works on time dependent string moduli and D-branes, referenced in [6], and earlier comments on the AdS/CFT correspondence in [56]).

Let us warm up by considering quantum field theory (no gravity) in situations with a moduli space of vacua, such as the $\mathcal{N}=4$ super Yang-Mills theory. In interacting field theories, generically there are points in the moduli space of a scalar field ϕ at which light fields χ_I appear, arising from an interaction of the form

$$g^2 \sum_{I=1}^{N_{\chi}} \phi^2 \chi_I^2. \tag{5.1}$$

This interaction produces a ϕ -dependent mass for χ , $m_{\chi} = g\phi$. When ϕ rolls around its moduli space, this results in a time dependent mass for the χ particles. When ϕ rolls toward $\phi = 0$, the χ particles become relevant to the dynamics of ϕ .

This can in general lead to two different effects: production of χ particles, and radiative corrections to ϕ 's effective action due to χ particles running in loops. The first effect, particle production, is controlled by a non-adiabaticity parameter $\dot{m}_{\chi}/m_{\chi}^2 \sim \dot{\phi}/(g\phi^2)$; the effect is roughly exponentially suppressed in the inverse of this parameter. The second effect, loop corrections to ϕ 's effective action, produce for example higher derivative corrections scaling as $N_{\chi}\dot{\phi}^2/\phi^4$. Thus at weak coupling, we expect particle production to dominate, and at strong 'tHooft coupling (large gN_{χ}), we expect the virtual corrections to dominate. This is indeed what happens, and in both limits the effects of the χ s back react in a simple but crucial way on the dynamics of ϕ .

At weak coupling, when ϕ rolls past the point $\phi = 0$ (say with an impact parameter μ) one finds a production of the following number density of χ particles:

$$n_{\chi} = \int \frac{d^3k}{(2\pi)^3} n_k = \frac{(gv)^{3/2}}{(2\pi)^3} e^{-\pi g\mu^2/v}$$
 (5.2)

and a corresponding energy density

$$\rho_{\chi} \sim n_{\chi} g |\phi(t)| \tag{5.3}$$

This energy density (5.3) traps ϕ near the origin, as discussed in detail in [6].

In the presence of gravity, the range over which ϕ 's kinetic energy dominates is limited by Hubble friction, and the trapping effect can be limited by dilution of created particles. However, there remains a nontrivial regime in which this effect persists and provides a vacuum selection mechanism, as well as a "trapped inflation" mechanism in which the field can be held temporarily on the side of a steep potential, producing accelerated expansion of the universe.

At strong 'tHooft coupling, one can use the AdS/CFT correspondence to analyze the physics [48]. The Coulomb branch of the theory (which in general is not a flat direction) is described on the gravity side by brane domain walls in AdS (which in general are time dependent solutions moving toward the horizon of the Poincare patch). On the gravity side, it is immediately clear from the geometry that it takes forever in the (super)gravity approximation for the domain wall to reach the origin. Up to back reaction limitations discussed in detail in [54], the dynamics of the scalar field describing the probe position is governed by the Dirac-Born-Infeld action, proportional to $1/\gamma \equiv 1/\sqrt{1-v_p^2}$ where $v_p^2 = N\dot{\phi}^2/\phi^4$ is the proper velocity of the probe. This leads to a dynamics in which the higher derivative terms in the action contribute crucially, slowing down the field velocity $\dot{\phi}$ proportionally to ϕ^2 as it approaches the origin, an effect dubbed "D-cceleration".

When coupled to gravity by embedding the system in a Calabi-Yau compactification, there are generically mass terms generated for ϕ and a corresponding closing up of the AdS throat at a finite nonzero warp factor in the IR [57]. This preserves a window in which the D-cceleration effect operates and produces inflation on a steep potential. The density perturbation spectrum, obtained by expanding the DBI action coupled to gravity, leads to distinctive predictions of this inflationary model coming from controlled but relatively large non-Gaussian contributions [54].

I include this brief review of velocity dependent effects because, aside from their intrinsic interest, it is important to account for them in determining the dynamics of the moduli. Putting together what we have learned here about the moduli potential and kinetic effects, and their relation to the microphysics of string theory, I hope you will be better prepared to attack the many important open problems that await us.

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