



“Micro SUSY”

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Reference: 2004 TASI lectures
[hep-th/0505029](https://arxiv.org/abs/hep-th/0505029)

A photograph of the LHC tunnel, showing a long row of blue superconducting magnets. A yellow laser line is visible on the magnets. The tunnel is dimly lit, with some lights on the right side.

SUSY + LHC = ?

Mediation mechanism
... maybe

Uncertainty principle:

depth \times breadth \leq 2 lectures

(Note sign!)

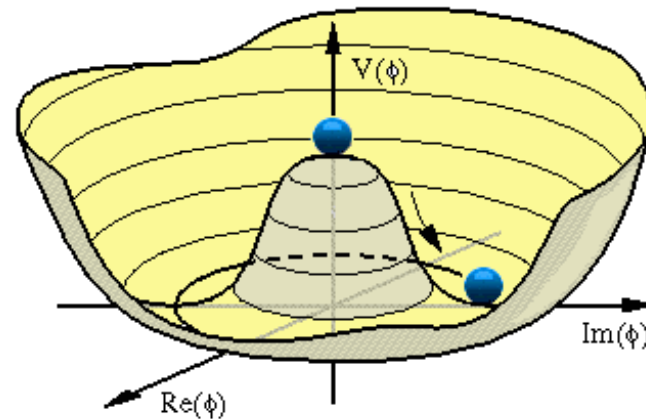
Help me saturate it: Ask questions!

Outline

- Direct SUSY breaking
- “UV mediation”
- SUSY flavor problem
- Gauge mediation
- Anomaly mediation
- High-scale SUSY breaking

Can we find the “Higgs” of SUSY breaking at LHC?

- $\langle F_\Phi \rangle \sim 100 \text{ GeV}$
- Couple Φ to MSSM via renormalizable operators
(no $1/M$ suppression)



Problems

- Gaugino masses too small

$$\Delta\mathcal{L} = \sqrt{2} g \langle H \rangle^\dagger \lambda \tilde{H} + \text{h.c.}$$

$$\Rightarrow M_{1,2} \sim M_{W,Z}$$

$$M_3 = 0$$

- Scalar masses too small

$$\Delta W = y Q \langle H \rangle u^c$$

$$\Rightarrow m_{\tilde{q}} = m_q$$

$$\Delta\mathcal{L} = y \tilde{Q} \langle F_H \rangle \tilde{u}^c + \text{h.c.}$$

$$\Rightarrow \pm \text{eigenvalues}$$

$$\Delta V_D = g^2 \langle D_3 \rangle \tilde{Q}^\dagger T_3 \tilde{Q}$$

$$\Rightarrow m_{\tilde{q}} \leq m_u \text{ at tree level} \quad (\text{Dimopoulos, Georgi})$$

Solutions



SUSY breaking mediated by

- Non-renormalizable interactions
(UV physics)
- Loops
- Supergravity

UV Mediation

SUSY broken by $\langle F_X \rangle \neq 0$

UV physics at M_{P} couples to visible sector

$$\begin{aligned}\mathcal{L}_{\text{eff}} &\sim \int d^4\theta \frac{1}{M_{\text{P}}^2} X^\dagger X Q^\dagger Q \\ &+ \int d^2\theta \frac{1}{M_{\text{P}}} X W^\alpha W_\alpha + \text{h.c.} \\ &+ \int d^2\theta \frac{1}{M_{\text{P}}} X Q H u^c + \text{h.c.} \\ &+ \dots\end{aligned}$$

$$\begin{aligned}
\Rightarrow \Delta\mathcal{L}_{\text{eff}} &\sim \frac{\langle F_X \rangle^2}{M_{\text{P}}^2} \tilde{Q}^\dagger \tilde{Q} && \text{scalar masses} \\
&+ \frac{\langle F_X \rangle}{M_{\text{P}}} \lambda^\alpha \lambda_\alpha + \text{h.c.} && \text{gaugino masses} \\
&+ \frac{\langle F_X \rangle}{M_{\text{P}}} \tilde{Q} H \tilde{u}^c + \text{h.c.} && A \text{ terms} \\
&+ \dots
\end{aligned}$$

All SUSY breaking masses of order

$$M_{\text{SUSY}} \sim \frac{\langle F_X \rangle}{M_{\text{P}}}$$

Even μ and $B\mu$ terms:

$$\Delta\mathcal{L}_{\text{eff}} \sim \int d^4\theta \frac{1}{M_{\text{P}}} X^\dagger H_u H_d + \text{h.c.}$$
$$+ \int d^4\theta \frac{1}{M_{\text{P}}^2} X^\dagger X H_u H_d + \text{h.c.}$$

$$\Rightarrow \Delta\mathcal{L}_{\text{eff}} \sim \int d^2\theta \frac{\langle F_X \rangle}{M_{\text{P}}} H_u H_d + \text{h.c.} \quad \mu \text{ term}$$

$$+ \frac{\langle F_X \rangle^2}{M_{\text{P}}^2} H_u H_d + \text{h.c.} \quad B\mu \text{ term}$$

Exercise

At sufficiently high order, all possible SUSY breaking terms are generated. Estimate the size of the difference between the fermion and scalar kinetic terms.

SUSY Flavor Problem

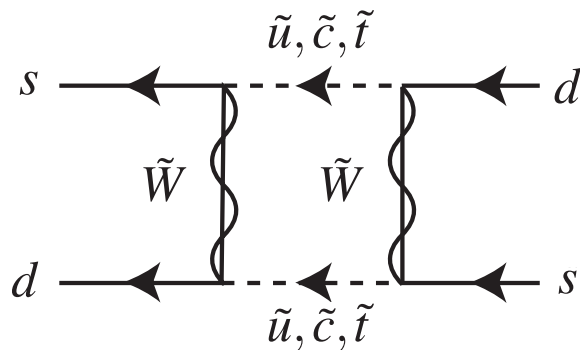
Flavor dependence of scalar masses:

$$\Delta\mathcal{L}_{\text{eff}} = \int d^4\theta \frac{c^i_j}{M_{\text{P}}^2} X^\dagger X Q_i^\dagger Q^j$$

$$\Rightarrow (m_{\tilde{Q}}^2)^i_j = \frac{c^i_j}{M_{\text{P}}^2} \langle F_X \rangle^2$$



E.g. $K^0 - \bar{K}^0$ mixing



$$\Rightarrow \frac{m_{\tilde{d}\tilde{s}}^2}{m_{\tilde{s}}^2} \lesssim 10^{-3} \left(\frac{m_{\tilde{s}}}{\text{TeV}} \right)$$



Isn't gravity flavor-blind?

IR: gravitons couple via equivalence principle
 \Rightarrow flavor-blind

UV: string/M theory

\Rightarrow UV states carry flavor

\Rightarrow flavor-violating effective operators

A Popular Ansatz

At $\mu = M_{\text{P}}$:

$m_0^2 =$ common scalar mass

$m_{1/2} =$ common gaugino mass

A terms $A_{ij} = A_0 y_{ij}$

$\mu, B\mu$ terms

Fix $\langle H \rangle = 256 \text{ GeV} \Rightarrow 4$ free parameters

$\sim 10^4$ papers

“Minimal SUGRA”

Hidden Sector Running

(Cohen, Roy, Schmaltz 2006)

$$\mathcal{L}_{\text{eff}} = \int d^4\theta \frac{A_i}{M_{\text{P}}^2} X^\dagger X Q^\dagger Q$$
$$+ \int d^4\theta \sum_{a=1}^3 \frac{B_a}{M_{\text{P}}} X W_a^\alpha W_{\alpha a} + \text{h.c.}$$
$$m_i^2 = \frac{A_i}{M_{\text{P}}^2} \langle F_X \rangle^2$$
$$M_a = \frac{B_a}{M_{\text{P}}} \langle F_X \rangle$$

X = dynamical field

$$\frac{dM_a}{dt} = \frac{b_a}{8\pi^2} g_a^2 M_a - \frac{1}{2} \gamma_X M_a$$
$$\gamma_X = \frac{d \ln Z_X}{dt}$$

$$\frac{dm_i^2}{dt} = \sum_{a=1}^3 \frac{C_{ai}}{2\pi^2} g_a^2 M_a^2 - \gamma_X m_i^2$$
$$t = \ln \mu$$

\Rightarrow weak scale masses depend on γ_X

Gaugino masses:

$$M_a(t) = \hat{M}_a(t) \exp \left\{ -\frac{1}{2} \int_0^t dt' \gamma_X(t') \right\}$$

$$\text{where } \hat{M}_a(t) = M_a(0) \exp \left\{ -\int_0^t dt' \frac{b_a}{8\pi^2} g_a^2(t') \right\}$$

= solution without hidden sector running

⇒ absorb hidden sector effects in overall scale

Scalar masses:

$$m_i^2(t) = -\sum_{a=1}^3 \frac{C_{ai}}{2\pi^2} \int_0^t dt' g_a^2(t') M_a^2(t') \exp \left\{ -\int_{t'}^t dt'' \gamma_X(t'') \right\} \\ - m_i^2(0) \exp \left\{ -\int_0^t dt' \gamma_X(t') \right\}$$

⇒ nontrivial hidden sector effects

Predictions independent of hidden sector:

$$S = \sum_i a_i m_i^2$$

$$\text{such that } \sum_i a_i C_{ia} = 0, \quad a = 1, 2, 3$$

$$\Rightarrow \frac{dS}{dt} = -\gamma_X S$$

$$S(t=0) = 0 \quad \Rightarrow \quad S(t) \equiv 0$$

$$\text{e.g.} \quad m_{\tilde{Q}}^2 - 2m_{\tilde{u}}^2 + m_{\tilde{d}}^2 - m_{\tilde{L}}^2 + m_{\tilde{e}}^2 = 0$$

Natural Flavor

$m_{\tilde{Q}}^2, m_{\tilde{u}}^2, m_{\tilde{d}}^2 \simeq$ diagonal

in basis that diagonalizes m_u, m_d

- $m_{\tilde{Q}}^2, m_{\tilde{u}}^2, m_{\tilde{d}}^2 \propto$ identity
- Special flavor structure
(*e.g.* Nir, Seiberg 1993)

Focus on first possibility

Requires flavor-blind messenger interaction



Gauge Mediation

Standard model gauge interactions flavor-blind

\Rightarrow natural messenger interaction

Messenger fields:

$\Phi, \tilde{\Phi}$ = vectorlike representation of standard model gauge group

$$\Delta\mathcal{L} = \int d^2\theta \lambda X \tilde{\Phi} \Phi + \text{h.c.}$$

$$\langle X \rangle \neq 0, \quad \langle F_X \rangle \neq 0$$

$$m_{1/2} \sim \text{[Diagram: wavy line, loop of } \Phi \text{, wavy line]} \sim \frac{g^2}{16\pi^2} \frac{F_X}{X}$$

$$m_0^2 \sim \text{[Diagram: dashed line, loop of } \Phi \text{, wavy lines]} \sim \left(\frac{g^2}{16\pi^2} \right)^2 \underbrace{\left| \frac{F_X}{X} \right|^2}_{U(1)_R \text{ invariant}}$$

- Independent of λ

$U(1)_R$ invariant

\Rightarrow masses fixed by gauge quantum numbers, F_X/X

- $\frac{F_X}{X} \sim 10 \text{ TeV}$

- $m_0 \sim m_{1/2}$

But: sign of m_0^2 ? Predictions?

Calculation of Masses

Use SUSY effective theory (Giudice, Rattazzi 1997)

$M \rightarrow \mathcal{M} = M + \theta^2 F =$ chiral superfield

How does effective theory below M depend on \mathcal{M} ?

$$\mathcal{L}_{\text{eff}} = \int d^4\theta Z Q^\dagger e^V Q + \left(\int d^2\theta \tau W^\alpha W_\alpha + \text{h.c.} \right) \\ + \text{higher-dimension operators}$$

Z, τ depend logarithmically on M via RG

$$\tau \sim \frac{g^2}{16\pi^2} \ln M \quad \Rightarrow [\tau]_{\theta^2} \neq 0 \quad \Rightarrow m_{1/2} \neq 0$$

$$Z \sim \frac{g^2}{16\pi^2} \ln M \quad \Rightarrow [Z]_{\theta^4} \neq 0 \quad \Rightarrow m_0^2 \neq 0$$

Gaugino mass:

$$\tau = \frac{1}{2g^2} + \theta^2 \frac{m_{1/2}}{g^2} = \text{chiral} \quad \Rightarrow \quad m_{1/2} = g^2 [\tau]_{\theta^2}$$

Matching and running:

$$\tau(\mathcal{M}) = \tau'(\mathcal{M})$$

$$\Rightarrow \tau(\mu) = \tau_0 + \frac{b'}{16\pi^2} \ln \frac{\mathcal{M}}{\Lambda} + \frac{b}{16\pi^2} \ln \frac{\mu}{\mathcal{M}}$$

$b - b' = N =$ number of messengers

$$\Rightarrow m_{1/2} = -\frac{g^2 N}{16\pi^2} \frac{F}{M}$$

Scalar mass:

$$\frac{d \ln Z}{d \ln \mu} = \frac{C}{4\pi^2} g^2$$

$$\Rightarrow \ln Z(\mu) = \ln Z_0 + \frac{2C}{b'} \ln \frac{g_0'^2}{g'^2(M)} + \frac{2C}{b} \frac{g^2(M)}{g^2(\mu)}$$

$Z = \text{real}$

$$\Rightarrow M \rightarrow |\mathcal{M}|,$$

$$g^2 \rightarrow \frac{1}{\tau + \tau^\dagger} \quad (\text{independent of } \Theta \propto \text{Im}(\tau))$$

$$\Rightarrow m^2(\mu = M) = \frac{g^4(M)}{(8\pi^2)^2} C N \left| \frac{F}{M} \right|^2 > 0$$

Finite 2-loop calculation done with 1-loop RG!

Exercise

Find effective operators that give corrections to the gaugino and scalar masses of order

$$\Delta m_{1/2} \sim \frac{F}{M} \times \frac{F^2}{M^4}$$

$$\Delta m_0^2 \sim \frac{F^2}{M^2} \times \frac{F^2}{M^4}$$

These are subleading for $F \ll M$

Exercise

Derive the formulas for the gaugino and scalar mass. Note that it is a bit surprising in this approach that the scalar mass comes in at two loops, since the anomalous dimension is one loop. Explain this.

Phenomenology

- $\frac{m_{\tilde{q}}}{m_{\tilde{e}}} \sim \sqrt{N_c} \frac{g_3^2}{g_1^2} \sim 10$

$$m_{\tilde{e}} \gtrsim 100 \text{ GeV} \Rightarrow m_{\tilde{q}} \gtrsim 1 \text{ TeV}$$

Good: $m_{h^0} > 114 \text{ GeV}$ Bad: tuned!

- Gravitino LSP

$$m_{3/2} \sim \frac{F_0}{M_{\text{P}}} \sim 100 \text{ GeV} \left(\frac{\sqrt{F_0}}{10^{10} \text{ GeV}} \right)^2$$

$F_0 = \text{fundamental scale of SUSY breaking} \gtrsim F$

Gravitino couplings suppressed by $1/F_0$ at low energies

\Rightarrow NLSP long-lived, can decay in detector

$$\text{e.g. } \chi^0 \rightarrow \gamma \tilde{G} \quad \text{or} \quad \tilde{\tau}_R \rightarrow \tau \tilde{\Gamma}$$

- Dark matter: super-WIMP scenario
NLSP freezes out,
late decay converts energy to gravitino
⇒ no direct detection

Anomaly Mediation

Gravity is flavor-blind
... in IR

Motivates SUSY breaking by
auxiliary fields of SUGRA

Part of graviton multiplet,
couplings dictated by super-covariance



“Need-to-know” SUGRA

$\mathcal{N} = 1$ SUGRA multiplet: $(g_{\mu\nu}, \psi_\mu, A_\mu, F_\phi)$

\Rightarrow SUSY breaking by $\langle F_\phi \rangle \neq 0$

Rules for F_ϕ couplings:

$U(1)_R \times$ scale transformations

\subset superconformal gauge symmetry

$\phi = \underbrace{1}_{\text{superconformal gauge choice}} + \theta^2 F_\phi = \text{chiral}$

$=$ “superconformal compensator”

Ordinary matter, gauge multiplets have $R = 0, d = 0$

$$R(\phi) = \frac{2}{3}, \quad d(\phi) = 1$$

$$\begin{aligned} \Rightarrow \mathcal{L} = & \int d^4\theta \phi^\dagger \phi K(Q, \dots) \\ & + \int d^2\theta \phi^3 W(Q, \dots) + \text{h.c.} \\ & + \int d^2\theta \tau W^\alpha W_\alpha + \text{h.c.} \end{aligned}$$

Integrating out ϕ gives SUGRA potential

Renormalizable theory:

$$\mathcal{L} = \int d^4\theta \phi^\dagger \phi Q^\dagger Q + \int d^2\theta \phi^3 (mQ^2 + \lambda Q^3) + \text{h.c.}$$

Define $\hat{Q} = \phi Q$

$$\Rightarrow \mathcal{L} = \int d^4\theta \hat{Q}^\dagger \hat{Q} + \int d^2\theta \left(\underbrace{\phi m \hat{Q}^2}_{\text{}} + \lambda \hat{Q}^3 \right) + \text{h.c.}$$

SUSY breaking \leftrightarrow scale symmetry breaking

Looks unpromising phenomenologically:

- $m_{1/2} = 0$
- μ term = only scale breaking
 \Rightarrow only H_u, H_d feel SUSY breaking

Loop corrections?

- scale symmetry broken
 \Rightarrow all SUSY breaking terms generated
- $\mu =$ SUSY breaking effect

Regulate:

$$\mathcal{L} = \int d^4\theta \hat{Q}^\dagger \left(1 + \frac{\partial^2}{\Lambda^2 \phi^\dagger \phi} \right) \hat{Q} \quad d(\partial_\mu) = 1$$
$$+ \int d^2\theta \lambda \hat{Q}^3 + \text{h.c.}$$

$$Z_0 = Z(\mu) + \frac{\lambda^2}{16\pi^2} \ln \frac{\mu}{\Lambda} + \dots$$
$$\rightarrow Z \left(\frac{\mu}{|\phi|} \right) + \frac{\lambda^2}{16\pi^2} \ln \frac{\mu}{\Lambda |\phi|} + \dots$$

Z_0 independent of μ , $\phi \Leftrightarrow$ no UV SUSY breaking

$$\Rightarrow \mu \rightarrow \frac{\mu}{|\phi|}$$

$$m_{1/2} = -\frac{\beta_g}{g} F_\phi$$

$$m_0^2 = -\frac{1}{4} \frac{d\gamma}{d \ln \mu} |F_\phi|^2$$

$$A = \frac{1}{\lambda} \frac{\beta_\lambda}{\lambda} F_\phi$$

Defines renormalization group trajectory

\Rightarrow SUSY breaking independent of UV physics

Exercise

Show that

$$\ln \mu \rightarrow \ln \mu - \frac{1}{2} (\theta^2 F_\phi + \text{h.c.}) . \quad (\text{no } \theta^4 \text{ component})$$

Show that this implies that anomaly mediated masses are 2-loop.

Verify the formulas for the anomaly mediated soft breaking terms.

UV Insensitivity

Prediction independent of SUSY thresholds

$$\frac{1}{g^2(\mu)} = \frac{1}{g_0^2} + \frac{b'}{8\pi^2} \ln \frac{M}{\Lambda} + \frac{b}{8\pi^2} \ln \frac{\mu}{M}$$

$$\Lambda \rightarrow \Lambda\phi, \quad M \rightarrow M\phi \quad \Lambda, M = \text{chiral}$$

$$\Rightarrow \tau(\mu) = \tau_0 + \frac{b'}{16\pi^2} \ln \frac{M}{\Lambda} + \frac{b}{16\pi^2} \ln \frac{\mu}{M\phi}$$

SUSY breaking still equivalent to $\mu \rightarrow \frac{\mu}{\phi}$

Same for scalar mass.

Can anomaly mediation dominate?

$$\text{SUGRA} \Rightarrow \langle F_\phi \rangle \lesssim \frac{F_0}{M_{\text{P}}}$$

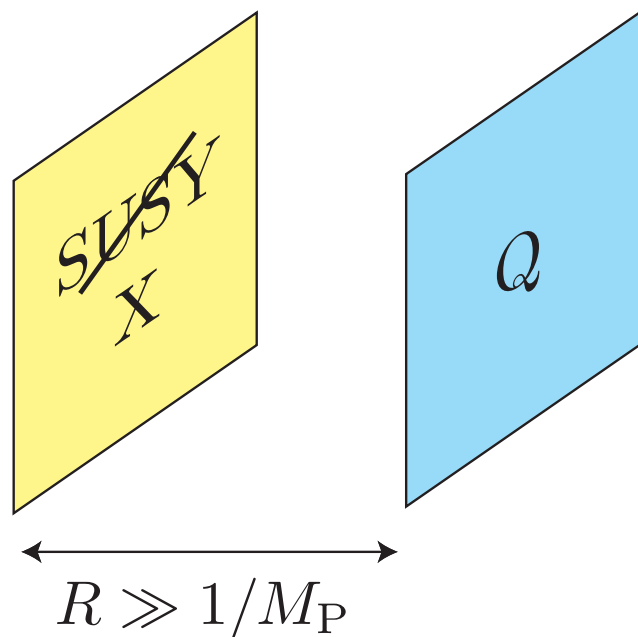
$$\Delta\mathcal{L}_{\text{eff}} \sim \int d^4\theta \frac{1}{M_{\text{P}}^2} X^\dagger X Q^\dagger Q$$

$$\Rightarrow \Delta m_0^2 \sim \left(\frac{F_0}{M_{\text{P}}} \right)^2 \gg \text{AMSB contribution}$$

Must forbid direct couplings to SUSY breaking

“sequestering”

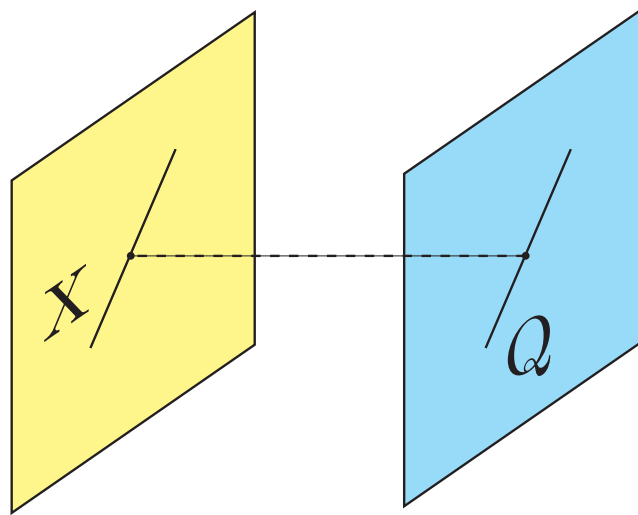
Brane-localized fields in extra dimensions



\Rightarrow Higher-dimensional theory cannot contain

$$\int d^4\theta X^\dagger X Q^\dagger Q$$

4D effective theory: must forbid generation of
 $\int d^4\theta X^\dagger X Q^\dagger Q$ from exchange of bulk fields

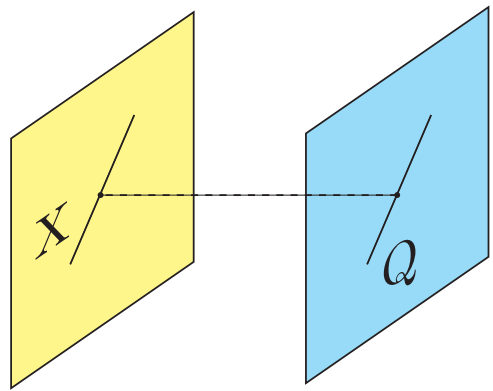


Bulk state has mass $M \gtrsim M_{\text{P}}$

\Rightarrow suppressed by $e^{-R/M} \ll 1$

Only light states ($M \lesssim 1/R$) contribute

Integrate out SUGRA KK modes: $M_{\text{KK}} \sim \frac{1}{R}$



$$\Rightarrow \Delta\mathcal{L}_4 \stackrel{?}{\sim} \underbrace{\frac{1}{M_5^3} \frac{1}{R}}_{\sim \frac{1}{M_{\text{P}}^2}} \int d^4\theta X^\dagger X Q^\dagger Q$$

In fact, in 4D effective theory $1/M_{\text{P}}^2$ contact terms are *required* by $\mathcal{N} = 1$ SUGRA

(Similar to D -term potential in gauge theory.)

Minimal model:

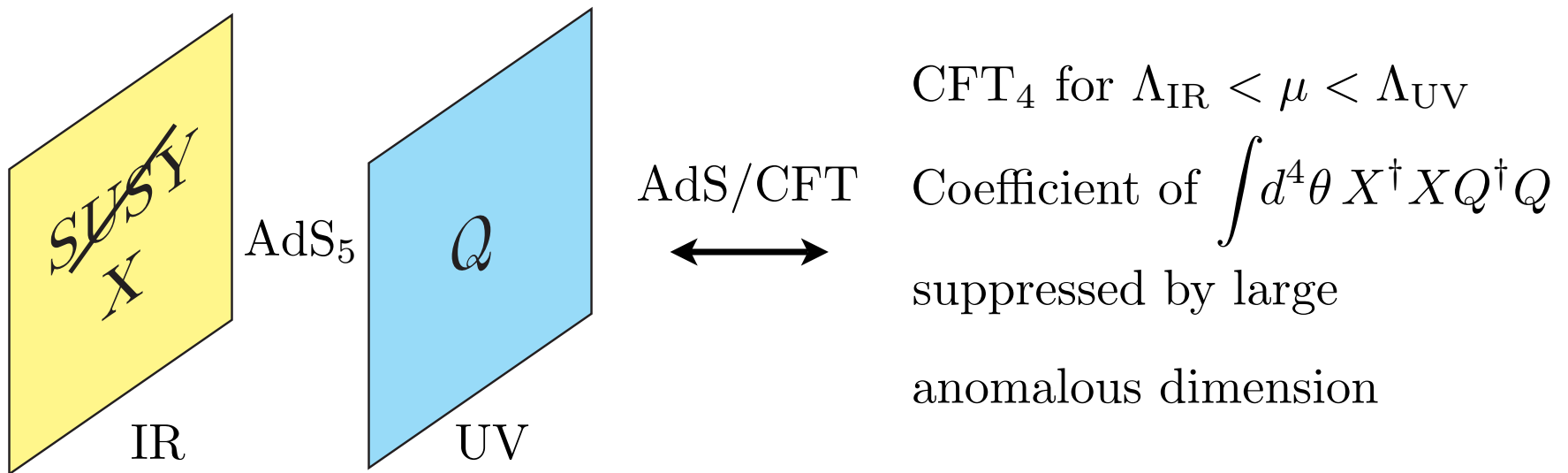
- 5D, minimal SUGRA in bulk
- Radion stabilized (crucial!)

Explicit calculation \Rightarrow sequestered Kähler potential

(Luty, Sundrum 1999)

Also, conformal sequestering:

(Luty, Sundrum 2001, 2002)



Is it Viable?

Sign of scalar mass:

$$\gamma = \frac{d \ln Z}{d \ln \mu} \sim +g^2 - y^2$$

$$m_0^2 \sim -\frac{d\gamma}{d \ln \mu} \sim -g\beta_g + y\beta_y$$

$$\Rightarrow m_0^2 > 0 \text{ requires } \beta_g < 0 \text{ or } \beta_y > 0$$

MSSM: $SU(2)_W$ and $U(1)_Y$ not asymptotically free,
no large Yukawa couplings for first two generations

$$\Rightarrow m_{\tilde{L}}^2, m_{\tilde{e}}^2 < 0!$$

“Gaugomaly” Mediation

(Pomarol, Rattazzi 1998)

Not all massive thresholds are supersymmetric

$$\mathcal{M} = M + \theta^2 F, \quad F \neq MF_\phi = \text{result of } M \rightarrow M\phi$$

Example: (Nelson, Weiner 2002)

$$\begin{aligned} \Delta\mathcal{L} &= \int d^4\theta c \phi^\dagger \phi^{-1} \tilde{\Phi}\Phi + \text{h.c.} & (\Phi, \tilde{\Phi} = \text{canonical}) \\ &= \int d^2\theta (c F_\phi) \phi^{-1} \tilde{\Phi}\Phi + \text{h.c.} \end{aligned}$$

$$c \sim 1 \Rightarrow M = cF_\phi \sim 10 \text{ TeV}$$

$$F = -MF_\phi \Rightarrow \Phi, \tilde{\Phi} \text{ act as gauge messengers}$$

Minimal model: $m_0^2 =$ anomaly-mediated at M

Non-minimal model OK (Hsieh, Luty 2007)

Exercise

Suppose we add to the visible sector

$$\Delta\mathcal{L} = \int d^4\theta X^\dagger X + \int d^2\theta \left[\lambda X \tilde{\Phi} \Phi + \frac{1}{M^{n-3}} X^n \right] + \text{h.c.}$$

Here Φ and $\tilde{\Phi}$ are in a vector-like representation of the standard model gauge group, and X is a singlet. Show that X effectively has a chiral superfield mass

$$\mathcal{M} = M + \theta^2 F$$

Compute M and F , and verify that $F \sim MF_\phi$, but $F \neq MF_\phi$. (Pomarol, Rattazzi 1998)

Phenomenology

- Spectrum depends on type of “gaugomaly” model
- $m_{3/2} \sim F_\phi \sim 10 \text{ TeV}$
⇒ conventional dark matter

Accidental SUSY

(Goh, Luty, Ng, 2003)

IR can have more symmetry than UV if all symmetry-breaking operators are irrelevant

“Accidental symmetry”

(*e.g.* baryon number in standard model)

Can “fundamental” symmetries (like Lorentz invariance or SUSY) be accidental? (Nielsen)

What about SUSY?

- Weak coupling \Rightarrow scalar mass relevant
 \Rightarrow need strong coupling
- Coupling must stay strong over a large range of scales for approximate SUSY
(We want to solve hierarchy problem!)
 \Rightarrow CFT

Does such a theory exist?

Existence

- Example: $\mathcal{N} = 4$ SYM with $N_c \gg 1$, $g^2 N_c \gg 1$
 \leftrightarrow string theory on $\text{AdS}_5 \times S_5$

$$d(\phi^\dagger \phi) \sim (g^2 N_c)^{1/4} \quad (\phi^\dagger \phi \leftrightarrow \text{string mode})$$

All relevant operators can be forbidden by $SO(6)$

- Another possible example (less SUSY)

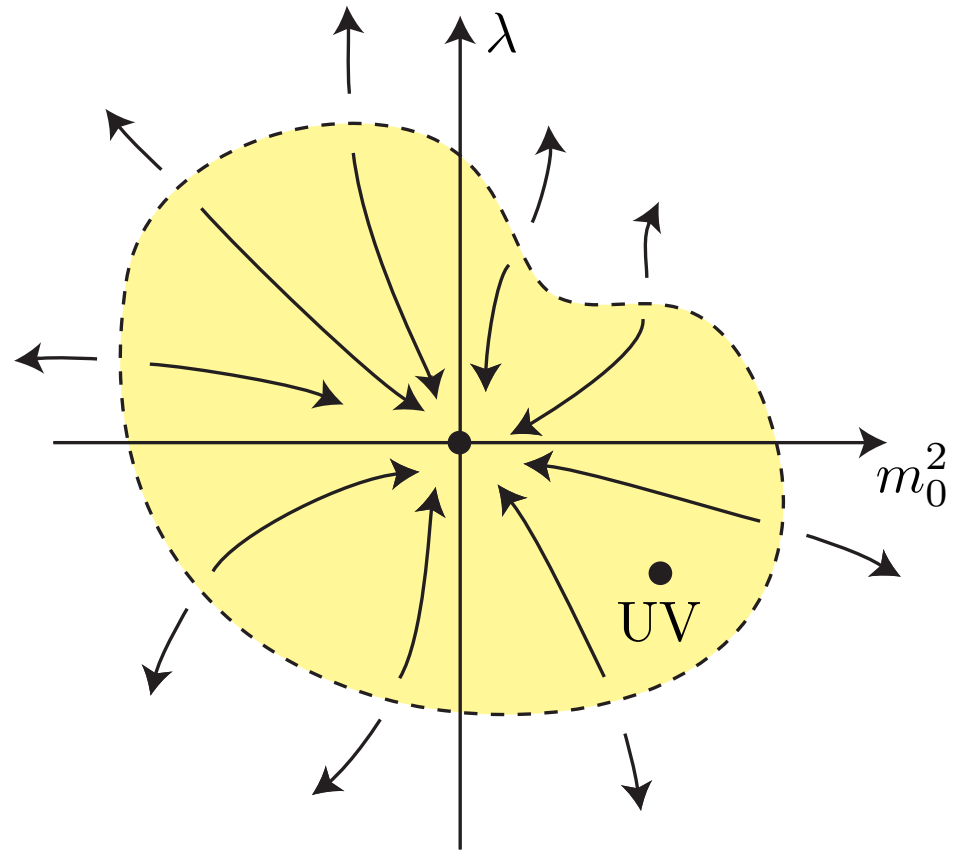
$$\mathcal{N} = 1 \text{ SUSY QCD with } N_c \sim N_f$$

\rightarrow strongly coupled CFT in IR

$$d(\phi^\dagger \phi) > 2 \quad (\text{Luty, Rattazzi 1999})$$

$$d(\phi^\dagger \phi) > 4?$$

Coupling constant flow:

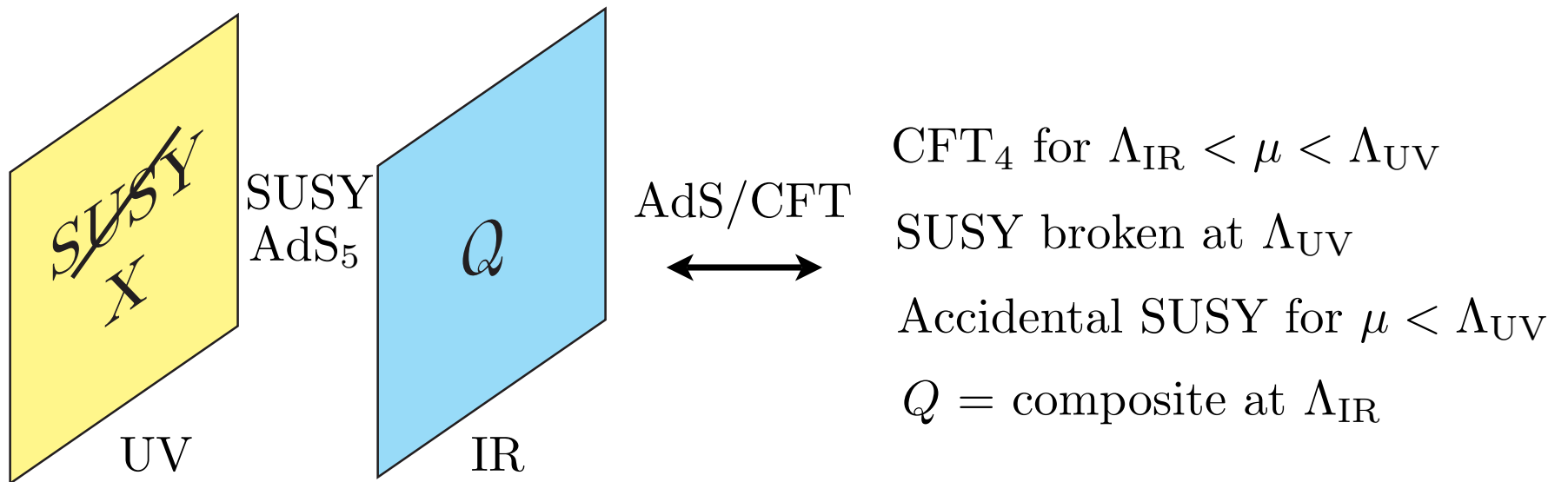


Realistic model must break conformal symmetry
at low energies (\gtrsim TeV)

\Rightarrow SUSY also broken

Fixed point never reached

Concrete realization in RS model:



Dilaton Potential

Exact IR SUSY \Rightarrow Flat dilaton potential

(AdS radion \leftrightarrow CFT dilaton)

\Rightarrow Get small dilaton potential from irrelevant SUSY breaking operators

$\sigma = \text{dilaton} \quad \langle \sigma \rangle = \Lambda_{\text{IR}}$

$$\Delta \mathcal{L}_{\text{CFT}} = \lambda \mathcal{O}_d \quad \Rightarrow \quad V_{\text{eff}} \sim \sigma^4 f \left(\frac{\lambda}{\sigma^{4-d}} \right)$$

$f(0) = 0$ (SUSY limit)

$$\Rightarrow V_{\text{eff}} \sim \sigma^d + \sigma^{2d-4} + \dots$$

$$V_{\text{eff}} \sim c_1 \sigma^{d_1} + c_2 \sigma^{d_2}$$

\Rightarrow metastable minimum

$$\langle \sigma \rangle \ll \Lambda_{\text{UV}} \text{ for } d_1 \simeq d_2 \quad (\text{log tuning})$$

SUSY is not exact in IR

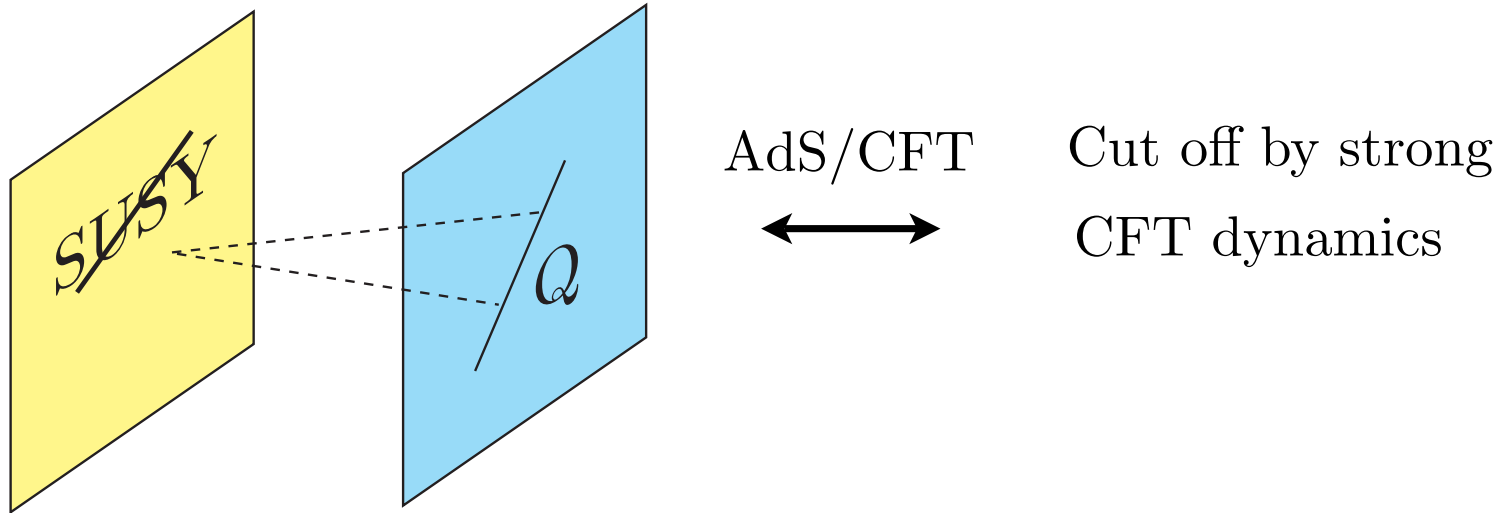
$$\frac{F_\sigma}{\sigma} \neq 0 \Rightarrow \text{anomaly mediated SUSY breaking!}$$

$$\text{RS} \Rightarrow \frac{F_\sigma}{\sigma} \sim \left(\frac{\Lambda_{\text{IR}}}{\Lambda_{\text{UV}}} \right)^{d_1 - 4} \Lambda_{\text{IR}} \quad (d_1 < d_2)$$

Model independent?

Gravity Loops

SUSY breaking from gravity loops



$$\Delta m_0^2 \sim \frac{1}{16\pi^2} \frac{1}{M_{\text{P}}^2} \Lambda_{\text{IR}}^4 \quad \Rightarrow \quad \Lambda_{\text{IR}} \lesssim 10^{11} \text{ GeV}$$

Standard model fields composite below M_{GUT} !

Low scale unification?

Conclusions

- SUSY flavor problem has elegant solutions
Gauge mediation, anomaly mediation, ...
- Predictions clouded by model-dependence
Predicting superpartner spectrum
 $\overset{?}{\leftrightarrow}$ postdicting fermion mass spectrum
- Look for new ideas